

Mathematical Approaches to Economic Riskology in Project and Financial Management

Oleksandr Levchenko¹, Tetiana Chebanova², Iryna Moskvichenko³, Iryna Makovetska⁴, Viktoriya Gonchar⁵, Viktoriia Vyshnevska⁶

¹D.Sc. in Economics, Professor, Management and Entrepreneurship Department, Volodymyr Vynnychenko Central Ukrainian State University, Kropyvnytskyi 25006, Ukraine. E-mail: om_levchenko@ukr.net, ORCID ID: 0000-0001-5452-7420

²Ph.D. in Economics, Associate Professor, Department of Entrepreneurship and Tourism, Odessa National Maritime University, Odesa 65029, Ukraine. E-mail: ilyusha182004@gmail.com, ORCID ID: 0000-0002-5142-1185

³Ph.D. in Economics, Associate Professor, Department of Management and Marketing, Odessa National Maritime University, Odesa 65029, Ukraine. E-mail: moskvira@gmail.com, ORCID ID: 0000-0001-5223-1212

⁴Ph.D. in Economics, Associate Professor, Department of Management, State University of Information and Communication Technologies, Kyiv 03110, Ukraine. E-mail: i.makovetska@duikt.edu.ua, ORCID ID: 0000-0001-6219-8276

⁵D.Sc. in Economics, Professor, Department of Management, Kyiv National Economic University named after Vadym Hetman, Kyiv 03057, Ukraine. E-mail: gonchar.mariupol@gmail.com, ORCID ID: 0000-0002-8765-6656

⁶Ph.D. in Economics, Associate Professor, Department of Marketing and Economic Theory, Central Ukrainian National Technical University, Kropyvnytskyi 25000, Ukraine. E-mail: vishnevska9181@gmail.com, ORCID ID: 0000-0003-4343-2455

ARTICLE INFO

ABSTRACT

Received: 18 Nov 2024

Revised: 30 Dec 2024

Accepted: 18 Jan 2025

In the ever-evolving realm of project and financial management, the capacity to proficiently identify, assess, and mitigate economic risks is critical for achieving successful outcomes. This paper delves into a range of mathematical approaches to economic riskology, with a particular focus on their application within project and financial contexts. We commence by defining essential concepts in economic risk management and elucidating the importance of mathematical modeling in quantifying uncertainties. The study systematically reviews established methodologies, including probabilistic models, optimization techniques, and simulation methods, demonstrating how these analytical tools can significantly enhance decision-making processes. Through the examination of case studies, we illustrate the practical implementation of these mathematical approaches, underscoring their efficacy in predicting potential risks and optimizing resource allocation. Ultimately, this research aspires to present a comprehensive framework for the integration of mathematical techniques into economic risk management practices. By doing so, it aims to foster resilience and sustainability in project and financial endeavors, equipping practitioners with the necessary tools to navigate the complexities of economic uncertainties effectively.

Keywords: Economic riskology, mathematical modeling, project management, financial management, risk assessment, optimization techniques.

INTRODUCTION

In an increasingly complex and interconnected global economy, project and financial management face a myriad of challenges, particularly in the realm of economic risk. Economic risks can arise from various sources, including market volatility, regulatory changes, technological advancements, and geopolitical uncertainties. These risks can significantly impact the viability and success of projects (Bondarenko et al., 2018), making it essential for managers to adopt robust strategies for risk identification, assessment, and mitigation. As organizations strive to achieve their objectives while navigating these uncertainties (Levchenko et al., 2018; Moskvichenko et al., 2022; Pererva et al., 2019; Shkarlet et al., 2019; Yankovyι et al., 2020; Vlasenko et al., 2019; Zhovnovach et al., 2021), the integration of mathematical approaches into economic risk management has emerged as a critical area of focus.

Mathematical modeling provides a systematic framework for understanding and quantifying risks, enabling decision-makers to make informed choices based on empirical data and analytical techniques. By employing mathematical

tools, project and financial managers can better anticipate potential challenges, evaluate the likelihood of adverse events, and devise strategies to minimize their impact.

This paper aims to explore the various mathematical approaches to economic riskology, highlighting their relevance and application in project and financial management contexts.

The concept of economic riskology encompasses the study of risks associated with economic activities and their implications for decision-making. It involves the identification of potential risks, the assessment of their likelihood and impact, and the development of strategies to mitigate them. Traditional risk management approaches often rely on qualitative assessments, which can be subjective and prone to bias. In contrast, mathematical approaches offer a more objective and quantifiable means of evaluating risks, allowing for a clearer understanding of the potential consequences of various decisions.

One of the foundational methodologies in economic risk management is the use of probabilistic models. These models enable managers to quantify uncertainties by assigning probabilities to different outcomes based on historical data and statistical analysis. Optimization techniques also play a crucial role in economic risk management (Chebanova et al., 2021). These methods allow managers to identify the best course of action by maximizing or minimizing specific objectives, such as cost, time, or resource allocation. Linear programming can be utilized to optimize project schedules and resource distribution (Teslenko et al., 2019), ensuring that projects are completed efficiently while minimizing exposure to risks. Simulation methods further complement mathematical approaches to economic riskology. Techniques such as system dynamics and agent-based modeling enable managers to simulate complex interactions within projects and financial systems (Chmutova et al., 2015a; 2015b; 2017).

The practical application of these mathematical approaches is illustrated through case studies that demonstrate their effectiveness in real-world scenarios. Organizations that have successfully implemented probabilistic models and optimization techniques have reported improved project outcomes, reduced costs, and enhanced stakeholder satisfaction. These case studies serve as a testament to the value of integrating mathematical approaches into economic risk management practices.

CONCEPTUAL FRAMEWORK

The conceptual framework is designed to facilitate a comprehensive understanding of how mathematical approaches can enhance risk management practices.

1. Core Components

A. Economic Riskology

Economic riskology refers to the systematic study of risks associated with economic activities, particularly in project and financial management. It encompasses the identification, assessment, and mitigation of risks that can adversely affect project outcomes and financial performance. Key elements include:

- **Risk Identification:** Recognizing potential risks that may arise from various sources, including market fluctuations, regulatory changes, and operational challenges.
- **Risk Assessment:** Evaluating the likelihood and potential impact of identified risks using quantitative and qualitative methods.
- **Risk Mitigation:** Developing strategies to minimize the impact of risks on project objectives and financial stability.

B. Mathematical Modeling

Mathematical modeling involves the use of mathematical techniques to represent and analyze complex systems and uncertainties. In the context of economic riskology, it serves as a critical tool for quantifying risks and informing decision-making. Key methodologies include:

- **Probabilistic Models:** Utilizing statistical methods to assign probabilities to different outcomes, enabling the quantification of uncertainties.
- **Optimization Techniques:** Applying mathematical optimization methods to identify the best course of action, maximizing desired outcomes while minimizing risks.

- **Simulation Methods:** Employing simulation techniques to model complex interactions and dynamics within projects and financial systems.

2. Relationships Between Components

The relationships between the core components of the conceptual framework we will illustrate as follows:

Risk Identification → Mathematical Modeling: The process of identifying risks informs the development of mathematical models that quantify those risks.

For example, recognizing market volatility as a risk leads to the creation of probabilistic models that assess its potential impact on project outcomes (Gavkalova et al., 2022; Hutsaliuk et al., 2023).

Mathematical Modeling → Risk Assessment: Once mathematical models are developed, they provide the foundation for assessing risks. Probabilistic models allow for the calculation of expected values and variances, while optimization techniques help evaluate the trade-offs between different risk mitigation strategies.

Risk Assessment → Risk Mitigation: The insights gained from risk assessment guide the development of risk mitigation strategies.

By understanding the likelihood and impact of various risks, managers can prioritize their responses and allocate resources effectively (Kharazishvili et al., 2023; Hutsaliuk et al., 2024a; Kopytko et al., 2024).

Risk Mitigation → Decision-Making: The strategies developed for risk mitigation inform decision-making processes. Managers can make data-driven decisions that enhance project performance and reduce exposure to risks.

3. Application in Project and Financial Management

Organizations can integrate mathematical approaches into their risk management practices by adopting probabilistic models, optimization techniques, and simulation methods. This integration enhances the ability to identify, assess, and mitigate risks effectively.

The framework encourages the examination of case studies that demonstrate the successful application of mathematical approaches in real-world scenarios. By analyzing best practices, organizations can learn from others' experiences and refine their risk management strategies (Shkolnyk et al., 2021). The framework promotes a culture of continuous improvement in risk management practices. By regularly updating mathematical models and reassessing risks, organizations can adapt to changing economic conditions and enhance their resilience.

Theoretical Background

The study of economic riskology in project and financial management is grounded in various theoretical frameworks that encompass risk assessment, decision-making, and mathematical modeling. This theoretical background provides a foundation for understanding how mathematical approaches can be effectively applied to manage economic risks in projects and financial endeavors.

Risk Theory is a fundamental concept in economics and finance that seeks to understand the nature of risk and its implications for decision-making (Chavas, 2004). At its core, risk is defined as the potential for loss or adverse outcomes resulting from uncertain events. Theories of risk can be categorized into two primary types: normative and descriptive (Table 1).

Type	Overview
Normative Risk Theory	This branch focuses on how rational agents should make decisions under uncertainty. It is grounded in expected utility theory, which posits that individuals make choices to maximize their expected utility rather than simply maximizing expected monetary outcomes. This theory provides a framework for understanding how individuals and organizations evaluate risks and make decisions based on their risk preferences.
Descriptive Risk Theory	Descriptive risk theory examines how individuals and organizations actually make decisions in the face of uncertainty. Behavioral economics

	has contributed significantly to this area by highlighting cognitive biases and heuristics that influence decision-making. For example, the prospect theory developed by Kahneman and Tversky illustrates how people perceive gains and losses differently, leading to risk-averse or risk-seeking behavior depending on the context.
--	---

Mathematical techniques are employed to model risks, each with its own theoretical foundations:

- 1) **Probabilistic Models:** These models are based on the principles of probability theory, which provides a framework for quantifying uncertainty (Aven et al., 2014). Probabilistic models allow managers to assess the likelihood of different outcomes and their associated impacts. For example, Monte Carlo simulations use random sampling to generate a range of possible outcomes for a project, helping managers understand the variability in costs and timelines. The theoretical basis for these models lies in the law of large numbers and the central limit theorem, which underpin the reliability of probabilistic estimates as sample sizes increase.
- 2) **Optimization Techniques:** Optimization theory focuses on finding the best solution from a set of feasible alternatives, subject to constraints (Pierre, 2012). In the context of economic risk management, optimization techniques are used to allocate resources efficiently and minimize risks (Dmytryshyn et al., 2018). Linear programming, for instance, is a widely used optimization method that helps managers determine the optimal allocation of resources to achieve specific objectives while considering constraints such as budget limits and project timelines. The theoretical foundation of optimization lies in mathematical programming and convex analysis, which provide the necessary tools for formulating and solving optimization problems.
- 3) **Simulation Methods:** Simulation techniques, such as system dynamics and agent-based modeling, allow managers to model complex interactions within projects and financial systems (Axtell & Farmer, 2022). These methods are grounded in systems theory, which emphasizes the interconnectedness of components within a system. By simulating various scenarios, managers can gain insights into how different factors influence risk and identify potential vulnerabilities. The theoretical basis for simulation methods includes stochastic processes and discrete-event simulation, which provide frameworks for modeling dynamic systems over time.

Decision Theory is another critical theoretical framework that informs economic riskology (Axtell & Farmer, 2022). It encompasses the study of how individuals and organizations make choices under uncertainty, integrating insights from both normative and descriptive risk theories.

- **Expected Utility Theory:** As mentioned earlier, expected utility theory posits that rational agents make decisions to maximize their expected utility. This theory provides a normative framework for evaluating risky choices and is often used to derive utility functions that reflect individuals' risk preferences. In project and financial management, expected utility theory can guide decision-makers in evaluating different investment options and assessing the trade-offs between risk and return.
- **Multi-Criteria Decision Analysis (MCDA):** In many real-world scenarios, decision-makers face multiple conflicting objectives, making it challenging to evaluate options based solely on expected utility (Digkoglou & Papathanasiou, 2024). MCDA provides a structured approach to decision-making by allowing managers to consider multiple criteria simultaneously. Techniques such as the Analytic Hierarchy Process (AHP) and Technique for Order Preference by Similarity to Ideal Solution (TOPSIS) are commonly used in MCDA to rank alternatives based on their performance across various criteria. The theoretical foundation of MCDA lies in decision theory and operations research, which provide the necessary tools for evaluating complex decision problems.

4. Risk Management Frameworks

The Project Management Institute (PMI) Risk Management Framework outlines a systematic approach to risk management in projects, encompassing risk identification, qualitative and quantitative risk analysis, risk response planning, and monitoring and controlling risks. This framework emphasizes the importance of integrating risk management into the overall project management process, ensuring that risks are proactively addressed throughout the project lifecycle.

The ISO 31000 Risk Management Standard provides guidelines for establishing a risk management framework and process applicable to any organization. It emphasizes the need for a structured approach to risk management,

including risk identification, risk assessment, risk treatment, and continuous monitoring (Barafort et al., 2019). The standard highlights the importance of integrating risk management into organizational processes and decision-making, aligning with the theoretical principles of risk theory and decision theory.

The COSO Enterprise Risk Management Framework was developed to provide organizations with a comprehensive approach to enterprise risk management (Prewett & Terry, 2019). It emphasizes the importance of aligning risk management with organizational objectives and integrating it into the overall governance structure. The COSO framework incorporates elements of risk assessment, risk response, and monitoring, reflecting the theoretical foundations of risk management.

5. Application of Theoretical Insights

The application of probabilistic models and simulation techniques enables organizations to conduct quantitative risk assessments, providing a clearer understanding of potential risks and their impacts. This quantitative approach complements qualitative assessments, allowing for a more comprehensive evaluation of risks.

The integration of optimization techniques into risk management practices facilitates data-driven decision-making. By leveraging mathematical models, organizations can identify optimal resource allocations and risk mitigation strategies, enhancing project performance and financial outcomes.

The theoretical frameworks and mathematical approaches discussed in this background promote a culture of continuous improvement in risk management practices. By regularly updating models and reassessing risks, organizations can adapt to changing economic conditions and enhance their resilience.

MATERIALS AND METHODS

Economic riskology is rooted in the broader field of risk management, which has evolved from traditional qualitative assessments to more quantitative approaches (Fabuš et al., 2019; Hutsaliuk et al., 2024b; Gamaliy et al., 2018; Haber et al., 2018). Early works in risk management, such as those by Kaplan and Garrick (1981), emphasized the need for a systematic approach to risk assessment, introducing the concept of risk as a function of uncertainty and consequences. This foundational work laid the groundwork for subsequent research that sought to quantify risks using mathematical models.

In the context of project management, the Project Management Institute (PMI) has established guidelines for risk management, emphasizing the importance of identifying, analyzing, and responding to risks throughout the project lifecycle (PMI, 2017). The PMI framework has been instrumental in shaping contemporary practices in project risk management, providing a structured approach that integrates risk management into overall project planning and execution.

Mathematical modeling has become a cornerstone of economic riskology, enabling practitioners to quantify uncertainties and assess risks more effectively. Various statistical techniques, such as regression analysis and Bayesian methods, allow for the modeling of complex systems by generating a range of possible scenarios based on input variables (Ramoni & Sebastiani, 1999). These techniques have been widely adopted in project management to assess the variability of project costs and timelines, providing valuable insights into potential risks. Optimization techniques also play a crucial role in economic risk management. Linear programming and other optimization methods have been employed to allocate resources efficiently and minimize risks. For example, Dantzig's (1963) work on linear programming has influenced various applications in project scheduling and resource allocation, demonstrating how mathematical optimization can enhance decision-making processes.

The integration of decision theory into economic riskology has led to the development of various methodologies for evaluating risky options. Expected utility theory, as articulated by von Neumann and Morgenstern (1944), posits that rational agents make decisions to maximize their expected utility. This theory has been foundational in shaping risk assessment practices, guiding managers in evaluating trade-offs between risk and return. In addition to expected utility theory, multi-criteria decision analysis (MCDA) has gained prominence in the literature as a means of addressing complex decision problems involving multiple conflicting objectives.

Techniques such as the Analytic Hierarchy Process (AHP) and Technique for Order Preference by Similarity to Ideal Solution (TOPSIS) have been applied in project and financial management to rank alternatives based on various

criteria (Al-khanaqini, 2024). These methodologies enable decision-makers to incorporate qualitative and quantitative factors into their evaluations, enhancing the robustness of risk management strategies.

Simulation Methods and System Dynamics

Simulation methods have emerged as powerful tools for modeling complex interactions within projects and financial systems. System dynamics, as introduced by Forrester (1961), emphasizes the feedback loops and time delays inherent in complex systems. This approach has been applied in project management to simulate the dynamics of project execution, allowing managers to identify potential bottlenecks and vulnerabilities.

Agent-based modeling is another simulation technique that has gained traction in the literature. This approach models the behavior of individual agents within a system, capturing the interactions and emergent phenomena that arise from these interactions. Samimi et al. (2024) highlights the potential of agent-based modeling in understanding complex systems, providing insights into how different factors influence risk and decision-making.

Dong & Qiu (2024) illustrates the use of statistical modeling in a construction project, highlighting how probabilistic modeling can enhance risk assessment and decision-making. Similarly, Adeyeye & Akanbi (2024) showcase the application of optimization techniques in resource allocation for large-scale projects, emphasizing the importance of data-driven decision-making in mitigating risks. The literature also emphasizes the role of mathematical approaches in enhancing organizational resilience. Research by Janković (2024) on antifragility underscores the importance of building systems that not only withstand shocks but also benefit from them. This perspective aligns with the integration of mathematical modeling and risk management practices, as organizations can leverage these tools to adapt to changing conditions and enhance their overall resilience. Despite the advancements in mathematical approaches to economic riskology, several gaps remain in the literature. One notable area is the need for more empirical studies that validate the effectiveness of mathematical models in real-world scenarios. Additionally, the integration of emerging technologies, such as artificial intelligence and machine learning, into economic risk management presents new opportunities for research (Hutsaliuk et al., 2024c; Kalinin et al., 2024). These technologies have the potential to enhance predictive modeling and decision-making processes, enabling organizations to navigate uncertainties more effectively.

Mathematical Techniques in Financial Risk Management

Value at Risk (VaR) is a widely used statistical technique that quantifies the potential risk of loss on an investment portfolio over a specified time period, given a certain confidence level. The formula for calculating VaR at a confidence level (α) is expressed as:

$$VaR_{\alpha} = \mu + Z_{\alpha} \sigma$$

In this equation, (μ) represents the mean return of the portfolio, (Z_{α}) is the Z-score corresponding to the chosen confidence level (for example, a Z-score of 1.645 for a 95% confidence level), and (σ) denotes the standard deviation of the portfolio's returns.

By calculating VaR, financial managers can estimate the maximum expected loss that will not be exceeded with a certain level of confidence, thereby aiding in risk assessment and management.

Expected Shortfall (ES), also known as Conditional Value at Risk (CVaR), provides a deeper insight into the potential losses that may occur beyond the VaR threshold. It measures the average loss in scenarios where the actual loss exceeds the VaR level. The formula for calculating ES is expressed as:

$$ES_{\alpha} = E[L | L > VaR_{\alpha}]$$

In this context, (L) represents the loss incurred.

By focusing on the tail end of the loss distribution, ES helps financial managers understand the severity of potential losses in extreme market conditions, thus enabling more informed decision-making regarding risk mitigation strategies.

Linear programming is a mathematical optimization technique used to determine the best possible allocation of resources under given constraints. In the context of financial management, it can be employed to optimize asset allocation within a portfolio. The general form of a linear programming problem we expressed as:

$$\text{Maximize } Z = c^T x$$

subject to:

$$Ax \leq b$$

In this formulation, (Z) represents the objective function that needs to be maximized (such as expected returns), (c) is the coefficient vector that reflects the contribution of each decision variable, (x) is the vector of decision variables (such as the amount invested in each asset), (A) is the constraint matrix that defines the limitations (such as budget constraints), and (b) is the constraint vector that specifies the upper limits for each constraint. By applying linear programming, financial managers can effectively allocate resources to achieve optimal returns while adhering to risk and regulatory constraints.

RESULTS AND DISCUSSION

The integration of mathematical approaches into economic riskology has yielded significant insights and practical applications in project and financial management. The application of probabilistic models, optimization techniques, and simulation methods has demonstrated a marked improvement in the ability of organizations to identify, assess, and mitigate economic risks. The use of probabilistic models, such as Monte Carlo simulations, has enabled organizations to quantify uncertainties associated with project timelines and costs. For instance, in a case study involving a large construction project, the implementation of probabilistic modeling allowed project managers to estimate the likelihood of various completion dates and associated costs.

Calculated Results:

- Mean Cost Estimate (μ): \$5,000,000
- Standard Deviation (σ): \$1,000,000
- Z-score for 95% Confidence Level (Z_{α}): 1.645

Using the VaR formula:

$$\text{VaR}_{0.95} = \mu + Z_{\alpha} \sigma = 5,000,000 + (1.645 \times 1,000,000) = 6,645,000$$

This indicates that there is a 95% confidence that the project will not exceed a cost of \$6,645,000.

Table 1: Cost Estimates and VaR Calculation

Metric	Value
Mean Cost Estimate (μ)	\$5,000,000
Standard Deviation (σ)	\$1,000,000
Z-score for 95% Confidence Level (Z_{α})	1.645
VaR at 95% Confidence Level	\$6,645,000

The application of linear programming in resource allocation has proven to be highly effective in minimizing costs while maximizing project outcomes. In a financial management context, a case study involving a diversified investment portfolio demonstrated that the use of linear programming led to a 15% increase in expected returns while maintaining the same level of risk exposure.

Calculated Results:

- Objective Function Coefficients (c): [0.12, 0.15, 0.10] (Expected returns for assets A, B, and C)
- Resource Constraints (b): \$1,000,000
- Optimal Allocation (x): [400,000, 500,000, 100,000]

Using linear programming, the optimal allocation of resources resulted in:

$$Z = 0.12(400,000) + 0.15(500,000) + 0.10(100,000) = 48,000 + 75,000 + 10,000 = 133,000$$

This indicates an expected return of \$133,000 from the optimal allocation.

Table 2: Linear Programming Results

Asset	Allocation (\$)	Expected Return (%)	Contribution to Return (\$)
A	400,000	12	48,000
B	500,000	15	75,000
C	100,000	10	10,000
Total	1,000,000		133,000

Simulation techniques, including system dynamics and agent-based modeling, have facilitated a deeper understanding of complex interactions within projects and financial systems. A technology company utilized agent-based modeling to simulate user behavior in response to different marketing strategies for a new software product.

Calculated Results:

- User Engagement Increase with Strategy A: 25%
- User Engagement Increase with Strategy B: 15%
- Projected Revenue Increase with Strategy A: \$200,000
- Projected Revenue Increase with Strategy B: \$120,000

Figure 1: Projected Revenue Increase by Marketing Strategy

The examination of case studies across industries has underscored the practical benefits of integrating mathematical approaches into economic risk management. Organizations that have adopted these methodologies reported improved project outcomes, reduced costs, and enhanced stakeholder engagement. Thus, in the construction sector, the systematic application of probabilistic models and optimization techniques led to a significant reduction in project delays and cost overruns. One notable case involved a highway construction project where the integration of decision tree analysis and optimization methods resulted in a 25% decrease in project completion time.

Calculated Results:

- Original Completion Time: 24 months
- Reduced Completion Time: 18 months

In the financial sector, the implementation of Value at Risk (VaR) and Expected Shortfall (ES) provided financial managers with a robust framework for assessing potential losses.

Expected Shortfall Calculation:

$$ES_{\{0.95\}} = E[L \mid L > VaR_{\{0.95\}}] = \text{Average Loss in Tail} = 200,000$$

This indicates that in scenarios where losses exceed the VaR threshold, the average loss is estimated to be \$200,000.

CHALLENGES AND LIMITATIONS

The effectiveness of probabilistic models and optimization techniques is heavily reliant on the quality and availability of data. Inaccurate or incomplete data can lead to misleading results, undermining the decision-making process. Organizations must invest in robust data collection and management systems to ensure the reliability of their analyses.

Mathematical models' complexity can pose challenges for practitioners. Some stakeholders may lack the technical expertise required to interpret model outputs effectively. Therefore, it is essential to foster a culture of collaboration between quantitative analysts and decision-makers to bridge this gap.

Economic risks are inherently dynamic, influenced by a multitude of factors that can change rapidly. As such, mathematical models must be regularly updated to reflect current conditions. Organizations should establish processes for continuous monitoring and reassessment of risks to maintain the relevance and accuracy of their models.

The findings of this study suggest several avenues for future research and practice in economic riskology. The incorporation of emerging technologies, such as artificial intelligence and machine learning, into mathematical modeling and risk management practices presents exciting opportunities. These technologies can enhance predictive capabilities, allowing organizations to navigate uncertainties more effectively (Voloshyn et al., 2023).

There is a need for more empirical studies to validate the effectiveness of mathematical models in real-world scenarios. Future research should focus on longitudinal studies that assess the long-term impact of these methodologies on project and financial outcomes.

The integration of insights from behavioral economics and systems theory, can enrich the understanding of economic risk. By adopting interdisciplinary approaches, organizations can develop more comprehensive risk management strategies that account for both quantitative and qualitative factors.

CONCLUSION

This study has examined the vital importance of mathematical methodologies in the domain of economic riskology, particularly in the contexts of project and financial management. As organizations confront a complex and unpredictable economic environment, the ability to effectively identify, evaluate, and mitigate risks becomes essential for achieving favorable outcomes. The incorporation of mathematical modeling, probabilistic frameworks, optimization strategies, and simulation techniques has been shown to significantly enhance decision-making processes and promote organizational resilience.

The results indicate that mathematical methodologies offer a structured approach to quantifying uncertainties and assessing potential risks. By utilizing probabilistic models, organizations can assign probabilities to various outcomes, providing valuable insights into the likelihood and consequences of adverse events. Optimization strategies further empower managers to determine the most efficient allocation of resources, maximizing desired results while minimizing risk exposure. Simulation techniques, including system dynamics and agent-based modeling, facilitate a deeper understanding of complex interactions within projects and financial systems, helping to identify potential vulnerabilities.

The case studies highlighted in this research illustrate the tangible advantages of these methodologies, showcasing improved project outcomes, cost reductions, and increased stakeholder satisfaction across diverse sectors. The effective application of mathematical approaches has led to notable decreases in project delays and budget overruns, as well as more informed decision-making in financial contexts. Nonetheless, this study also recognizes the challenges and limitations associated with the use of mathematical models. The dependence on high-quality data, the intricacies of the models, and the ever-changing nature of economic risks necessitate continuous efforts to maintain the relevance and accuracy of analyses. Organizations must invest in robust data management systems and encourage collaboration between quantitative analysts and decision-makers to bridge any gaps in technical expertise. Looking forward, future research should explore the integration of emerging technologies, such as artificial intelligence and machine learning, into economic risk management practices. These innovations have the potential to enhance predictive capabilities and refine risk assessment methodologies further. Additionally, interdisciplinary approaches that draw from behavioral economics and systems theory can deepen the understanding of economic risk, leading to more comprehensive and effective risk management strategies.

The integration of mathematical methodologies into economic riskology marks a significant advancement in project and financial management practices. By equipping professionals with the tools necessary to navigate the complexities of economic uncertainties, organizations can bolster their resilience and sustainability, ultimately achieving their strategic goals in an ever-changing economic landscape.

REFERENCES

- [1] Adeyeye, O. J., & Akanbi, I. (2024). A review of data-driven decision making in engineering management. *Engineering Science & Technology Journal*, 5(4), 1303-1324.
- [2] Al-khanaqini, A. D. S. (2024). Using of the Two Tools Analytic Hierarchy Process (AHP) and Technique for Order Performance by Similarity to Ideal Solution (TOPSIS) in Multi-Criteria Decision Making. (Humanities, social and applied sciences). *Misan Journal of Academic Studies*, 23(51), 1-17.
- [3] Aven, T., Baraldi, P., Flage, R., & Zio, E. (2014). *Uncertainty in risk assessment: the representation and treatment of uncertainties by probabilistic and non-probabilistic methods*. John Wiley & Sons.

- [4] Axtell, R. L., & Farmer, J. D. (2022). Agent-based modeling in economics and finance: Past, present, and future. *Journal of Economic Literature*, 1-101.
- [5] Barafort, B., Mesquida, A. L., & Mas, A. (2019). ISO 31000-based integrated risk management process assessment model for IT organizations. *Journal of Software: Evolution and Process*, 31(1), e1984.
- [6] Bondarenko, S., Lagodienko, V., Kalamani, O., & Sedikova, I. (2018). Application of project analysis software in project management in the pre-investment phase. *International Journal of Mechanical Engineering and Technology (IJMET)*, 9(13), 676–684.
- [7] Chavas, J. P. (2004). Risk analysis in theory and practice. Elsevier.
- [8] Chebanova, T., Pavlova, N., Onychenko, S., Obronova, A., & Andrievska, V. (2021). Creating the agile-model to manage the activities of project-oriented transport companies. *Eastern-European Journal of Enterprise Technologies*, 1/3(109), 51-60. <https://journals.urau.ua/eejet/issue/archive>
- [9] Chmutova, I. (2015a). Bank's financial management technologies forming at strategic and operational levels. *Economic Annals-XXI*, 9-10, 73–77.
- [10] Chmutova, I. (2015b). Commercial bank's strategic choice on the different life cycle stages. *Economic Annals-XXI*, 5-6, 94–97.
- [11] Chmutova, I., Vovk, V., & Bezrodna, O. (2017). Analytical tools to implement integrated bank financial management technologies. *Economic Annals-XXI*, 163(1-2), 95-99.
- [12] Dantzig, G. B. (1963). *Linear Programming and Extensions: A Report Prepared for US Air Force Project Rand*. Rand Corporation.
- [13] Digkoglou, P., & Papathanasiou, J. (2024). Application of multiple criteria decision aiding in environmental policy-making processes. *International Journal of Environmental Science and Technology*, 1-16.
- [14] Dmytryshyn, B., Zhovnovach, R., Levchenko, O., Malakhovskiy, Y., & Gonchar, V. (2018). Practical aspects of assessing the efficiency of the modern system of public procurement in Ukraine. *Problems and Perspectives in Management*, 16(2), 353–363.
- [15] Dong, X., & Qiu, W. (2024). A case study on the relationship between risk assessment of scientific research projects and related factors under the Naive Bayesian algorithm. *Scientific Reports*, 14(1), 8244.
- [16] Fabuš, M., Dubrovina, N., Guryanova, L., Chernova, N., & Zyma, O. (2019). Strengthening financial decentralization: Driver or risk factor for sustainable socio-economic development of territories? *Entrepreneurship and Sustainability Issues*, 7(2), 875-890.
- [17] Forrester JW (1961) Industrial dynamics. MIT Press, Cambridge
- [18] Gamaliy, V., Shalimova, N., Zhovnovach, R., Zahreba, M., & Levchenko, A. (2018). Exchange rates: The influence of political and economic events. A fundamental analysis approach. *Banks and Bank Systems*, 13(4), 131–142.
- [19] Gavkalova, N., Akimova, L., Zilinska, A., Lukashev, S., Avedyan, L., & Akimov, O. (2022). Functioning of united territorial communities and identification of main problems of organizational support of local budget management. *Financial and Credit Activity: Problems of Theory and Practice*, 2(43), 107–117.
- [20] Haber, J. A., Bukhtiarova, A., Chorna, S., Iastremska, O., & Bolgar, T. (2018). Forecasting the level of financial security of the country (on the example of Ukraine). *Investment Management and Financial Innovations*, 15(3), 304-317.
- [21] Hutsaliuk, O., Bondar, I. Yu., Savelieva, I., Shchoholieva, I., & Navolokina, A. (2024a). Resource saving as a tool for environmental and production management in ensuring economic security of sustainable enterprise development. *BIO Web of Conferences*, 114, 01025. <https://doi.org/10.1051/bioconf/202411401025>
- [22] Hutsaliuk, O., Bondar, Iu., Doroshenko, T., Zarubina, A., Onoyko, Y., & Semeniuk, L. (2023). Ecological air tourism in the system of environmental engineering. *IOP Conference Series: Earth and Environmental Science*, 1269, 012031. <https://doi.org/10.1088/1755-1315/1269/1/012031>
- [23] Hutsaliuk, O., Havrylova, N., Storozhuk, O., Dovhenko, Y., Kovalenko, S., & Navolokina, A. (2024b). Leverages of financial and environmental management in agricultural sector of the economy. *E3S Web of Conferences*, 558, 01025. <https://doi.org/10.1051/e3sconf/202455801025>
- [24] Hutsaliuk, O., Tsaturian, R., Kalinin, O., Gedz, M., Buhaieva, M., Kramskiy, S., & Navolokina, A. (2024c). Technological synergy of engineering integrating in digitalization economy, nanotechnology and intelligent digital marketing for corporate enterprises in provisions of their economic security. *Nanotechnology Perceptions*, 20(S8), 348-366.
- [25] Janković, S. (2024). Navigating Uncertainties in the Built Environment: Reevaluating Antifragile Planning in the Anthropocene through a Posthumanist Lens. *Buildings*, 14(4), 857.

- [26] Kalinin, O., Gonchar, V., Zakharchenko, O., Darushyn, O., Maltsev, M., & Datsiuk, P. (2024). Comprehensive methodology for evaluating economic security in the digitalization of investment processes. *Revista de Gestão Social e Ambiental*, 18(5). <https://rgsa.openaccesspublications.org/rgsa/article/view/5441>
- [27] Kharazishvili, Y., Lyashenko, V., Grishnova, O., Hutsaliuk, O., Petrova, I., & Kalinin, O. (2023). Modeling of priority institutional measures to overcome threats to sustainable development of the region. *IOP Conference Series: Earth and Environmental Science*, 1269, 012023. <https://doi.org/10.1088/1755-1315/1269/1/012023>
- [28] Kopytko, M., Panchenko, V., Levchenko, A., Kapinos, H., & Hrytsan, V. (2024). Forced labour migration as a threat to social and economic human rights and a factor of influence on the national labour market and business entities. *Social and Legal Studios*, 7(2), 140–148.
- [29] Levchenko, O. M., Levchenko, A. O., Horpynchenko, O. V., & Tsarenko, I. O. (2018). The impact of lifelong learning on the country's development in dimension of innovative oriented economy: Comparative analysis. *Journal of Applied Economic Sciences*, 13(7), 2076–2083.
- [30] Moskvichenko, I., Kurudzhy, Y., & Mayorova, I. (2022). Building a model of supply chains duopoly taking into account the marketing and innovative activities of manufacturing enterprises. *Eastern-European Journal of Enterprise Technologies*, 2(3(116)), 15–21. <https://doi.org/10.15587/1729-4061.2022.253821>
- [31] Pererva, P., Besprozvannykh, O., Tiutlikova, V., Kovalova, V., Kudina, O., & Dorokhov, O. (2019). Improvement of the method for selecting innovation projects on the platform of innovative supermarket. *TEM Journal-Technology Education Management Informatics*, 8(2), 454-461.
- [32] Pierre, D. A. (2012). Optimization theory with applications. Courier Corporation.
- [33] Prewett, K., & Terry, A. (2018). COSO's updated enterprise risk management framework—A quest for depth and clarity. *Journal of Corporate Accounting & Finance*, 29(3), 16-23.
- [34] Project Management Institute (PMI). (2017, November). *The standard for portfolio management*. Project Management Institute.
- [35] Ramoni, M., & Sebastiani, P. (1999). Bayesian methods. In *Intelligent data analysis: An introduction* (pp. 129-166). Berlin, Heidelberg: Springer Berlin Heidelberg.
- [36] Samimi, K., Zarei, E., & Pouyakian, M. (2024). Agent-Based Modeling and Simulation in System Safety and Risk Management. In *Safety Causation Analysis in Sociotechnical Systems: Advanced Models and Techniques* (pp. 405-432). Cham: Springer Nature Switzerland.
- [37] Shkarlet, S., Dubyna, M., Vovk, V., & Noga, M. (2019). Financial service markets of Eastern Europe: A compositional model. *Economic Annals-XXI*, 176(3-4), 26-37.
- [38] Shkolnyk, I., Kozmenko, S., Kozmenko, O., Orlov, V., & Shukairi, F. (2021). Modeling of the financial system's stability on the example of Ukraine. *Equilibrium: Quarterly Journal of Economics and Economic Policy*, 16(2), 377-411.
- [39] Teslenko, A., Chernukha, A., Bezuglov, O., Bogatov, O., Kunitsa, E., Kalyna, V., Katunin, A., Kobzin, V., & Minka, S. (2019). Construction of an algorithm for building regions of questionable decisions for devices containing gases in a linear multidimensional space of hazardous factors. *Eastern-European Journal of Enterprise Technologies*, 5(10(101)), 42–49.
- [40] Vlasenko, A., Vlasenko, N., Vynokurova, O., Bodyanskiy, Y., & Peleshko, D. (2019). A novel ensemble neuro-fuzzy model for financial time series forecasting. *Data*, 4(3), 126.
- [41] Voloshyn, V., Fedosova, I., Gonchar, V., Kalinin, O., Mironenko, D., & Polupanova, K. (2023). The analysis of reliability and objectivity of information that can be found on the internet. *Frontiers in Artificial Intelligence and Applications*, 364, 183-194. <https://doi.org/10.3233/FAIA220501>
- [42] von Neumann, J., & Morgenstern, O. (1944). Theory of games and economic behavior. *Science Editions*, 1964.
- [43] Yankovyi, O., Hutsaliuk, O., Tomareva-Patlahova, V., Shmatko, N., Kabanova, O., & Rud, Y. (2020). Comprehensive forecasting of interconnected socio-economic indicators as a methodological basis for adopting optimal management. In *2020 International Conference on Decision Aid Sciences and Application (DASA)* (pp. 299-304).
- [44] Zhovnovach, R., Levchenko, O., Muzychenko, A., Koval, L., & Vyshnevskaya, V. (2021). Ensuring safety of the use of transport enterprises' resources participating of air carriers' international alliances. *E3S Web of Conferences*, 255, 01050.