

A Plithogenic-Neutrosophic Perspective on Marketing Strategy: Unifying Fuzzy MCDM, TOPSIS, and DEMATEL

Igno Mary.I¹, S. Sandhiya^{2*}

¹ Research Scholar, Department of Mathematics,

² Assistant Professor, Department of Mathematics,

^{1,2*} Vels Institute of Science, Technology and Advanced Studies,(VISTAS),Pallavaram
Chennai, Tamilnadu

ARTICLE INFO

ABSTRACT

Received: 26 Dec 2024

Revised: 14 Feb 2025

Accepted: 22 Feb 2025

This paper explores the application of fuzzy Multi-Criteria Decision-Making (MCDM) methods, specifically TOPSIS and DEMATEL, within a neutrosophic framework to address complex decision-making problems in marketing strategies. Traditional MCDM methods often face challenges when dealing with conflicting criteria and uncertain data. To overcome these limitations, fuzzy MCDM methods, leveraging the principles of fuzzy set theory, offer a more flexible and nuanced approach. This study focuses on the evaluation of 15 marketing strategy alternatives across 13 criteria, integrating fuzzy and neutrosophic methods to handle uncertainty and vagueness effectively.

TOPSIS is highlighted for its effectiveness in quickly identifying the best alternatives by measuring their proximity to an ideal solution. DEMATEL, on the other hand, is recognized for its strength in modeling causal relationships among criteria, which is crucial in understanding interdependencies in decision-making contexts. By integrating neutrosophic values, which accommodate degrees of truth, falsity, and indeterminacy, both methods are adapted to handle greater levels of uncertainty. The study presents a comparative analysis of these methods, demonstrating their advantages in different scenarios.

The results provide insights into the relative strengths of TOPSIS and DEMATEL, particularly in handling indeterminacy, computational efficiency, and accuracy in ranking alternatives. The findings suggest that while TOPSIS is suitable for straightforward ranking tasks, DEMATEL offers deeper insights into the interplay between criteria. This study concludes by underscoring the potential of neutrosophic MCDM methods in enhancing decision-making across various fields, suggesting avenues for future research to further develop and refine these approaches.

Keywords:

INTRODUCTION

In decision science, Multi-Criteria Decision-Making (MCDM) methods have been developed to assist decision-makers in evaluating and ranking alternatives across multiple criteria[1]. MCDM approaches date back to the mid-20th century, with significant advancements in the late 1960s and 1970s[2]. These methods evolved to address real-world decision problems where various criteria often conflict, and exact data is not always available. Among the various types of MCDM techniques, fuzzy MCDM methods, introduced in the 1970s, have gained prominence for their ability to handle uncertainty and vagueness in decision-making. Fuzzy set theory, introduced by Lotfi Zadeh in 1965[3], [4], plays a crucial role in these methods by allowing for degrees of membership rather than binary true/false evaluations. Several fuzzy MCDM methods have been developed over the decades, including Fuzzy TOPSIS, Fuzzy DEMATEL, and other approaches like Fuzzy AHP (Analytic Hierarchy Process) and Fuzzy VIKOR (VlseKriterijumska Optimizacija I Kompromisno Resenje).

Among these, TOPSIS (Technique for Order of Preference by Similarity to Ideal Solution) and DEMATEL (Decision Making Trial and Evaluation Laboratory) have emerged as highly effective methods for handling complex decision problems that involve uncertain, imprecise, and fuzzy data[5]. TOPSIS is particularly useful for ranking alternatives by comparing their relative closeness to an ideal solution, making it a preferred method when the goal is to identify the best alternative quickly and efficiently. DEMATEL, on the other hand, excels in situations where understanding

the interrelationship between criteria is crucial, as it identifies and analyzes the cause-and-effect relationships among the criteria. Both methods are highly suitable for neutrosophic MCDM frameworks, which extend fuzzy logic to handle even greater uncertainty by incorporating truth, falsity, and indeterminacy values. Given the complexity of decision problems that arise in fields such as marketing strategy, where multiple alternatives and criteria must be evaluated, TOPSIS and DEMATEL stand out as the most suitable methods for providing accurate and insightful rankings and analyses under conditions of uncertainty[6], [7].

This paper focuses on utilizing these two methods within a neutrosophic framework for solving MCDM problems related to marketing strategies, where 15 alternatives are evaluated across 13 criteria[8]. The structure of this paper begins with the preliminaries of the TOPSIS algorithm, where its mathematical foundation and procedural steps for solving MCDM problems using ideal solutions are discussed. The necessary modifications for integrating neutrosophic values into the decision matrix are also outlined. Following this, the preliminaries of the DEMATEL algorithm are explored, with an emphasis on its capability to model the causal relationships between criteria. The next section delves into the formation of the normal decision matrix, where linguistic terms and uncertainty values are used to create neutrosophic decision matrices. These matrices are then normalized and weighted for both TOPSIS and DEMATEL methods.

In the comparative analysis section, a detailed comparison is made between DEMATEL and TOPSIS, examining their respective strengths in handling indeterminacy, computational efficiency, and ranking accuracy. This section includes a derivation of influence relationships in DEMATEL and the ideal distance metrics in TOPSIS[9], [10]. The subsequent section presents the rankings and results of both methods, demonstrating their performance in ranking the 15 alternatives across the 13 criteria. Finally, the paper concludes by discussing the implications of applying neutrosophic MCDM methods to marketing strategy development, highlighting the strengths and limitations of both TOPSIS and DEMATEL in different decision-making contexts. Suggestions for future research include enhancing these methods to address more complex and dynamic decision problems, further expanding the application of neutrosophic MCDM approaches.

Dematel and TOPSIS: Preliminaries, Equations, and Algorithms

DEMATEL (Decision-Making Trial and Evaluation Laboratory)

Preliminaries

DEMATEL is a method used to analyze and model complex causal relationships among factors. It is particularly helpful in identifying the key influencing and influenced factors in a system[11], [12].

Key steps involved in DEMATEL:

1. Constructing the direct-relation matrix.
2. Normalizing the direct-relation matrix.
3. Calculating the total relation matrix.
4. Determining the influence degree and the influenced degree.
5. Mapping the causal diagram.

The DEMATEL method allows for both direct and indirect influences to be captured, providing a better understanding of interrelationships in complex systems.

Equations

1. Direct-Relation Matrix (D):

$D = [d_{ij}]$, where d_{ij} is the degree of influence that factor i has on factor j .

2. Normalized Direct-Relation Matrix (X):

$X = D / \max(\sum d_{ij})$, where $\max(\sum d_{ij})$ is the largest row sum in D .

3. Total Relation Matrix (T):

$T = X (I - X)^{-1}$, where I is the identity matrix.

4. Influencing and Influenced Degrees:

a. The degree to which factor i influences other factors is $r_i = \sum T_{ij}$.

b. The degree to which factor i is influenced by other factors is $c_i = \sum T_{ji}$.

5. Causal Diagram:

Using $(r_i + c_i)$ and $(r_i - c_i)$, the causal diagram can be constructed.

Algorithm

1. Define the criteria or factors and gather expert opinions to construct the initial direct-relation matrix.

2. Normalize the direct-relation matrix.

3. Calculate the total relation matrix.

4. Determine the influence and influenced degrees (r_i and c_i).

5. Draw the causal diagram using the values of $(r_i + c_i)$ and $(r_i - c_i)$.

TOPSIS (Technique for Order Preference by Similarity to Ideal Solution)

Preliminaries

TOPSIS is a multi-criteria decision-making method. It is based on the concept that the best solution should have the shortest distance from the positive ideal solution (PIS) and the farthest distance from the negative ideal solution (NIS)[13].

Key steps involved in TOPSIS:

1. Constructing the decision matrix.

2. Normalizing the decision matrix.

3. Constructing the weighted normalized decision matrix.

4. Identifying the positive ideal solution (PIS) and negative ideal solution (NIS).

5. Calculating the separation measures for PIS and NIS.

6. Computing the relative closeness to the ideal solution.

7. Ranking the alternatives.

Equations

1. Normalized Decision Matrix:

$R = [r_{ij}]$, where $r_{ij} = x_{ij} / \sqrt{\sum x_{ij}^2}$ for $i=1,2,\dots,m$ and $j=1,2,\dots,n$.

2. Weighted Normalized Decision Matrix:

$V = [v_{ij}]$, where $v_{ij} = w_j * r_{ij}$, and w_j is the weight of the j -th criterion.

3. Positive Ideal Solution (PIS) and Negative Ideal Solution (NIS):

PIS: $A^+ = \{v_1^+, v_2^+, \dots, v_n^+\}$, where $v_j^+ = \max(v_{ij})$ for benefit criteria and $\min(v_{ij})$ for cost criteria.

NIS: $A^- = \{v_1^-, v_2^-, \dots, v_n^-\}$, where $v_j^- = \min(v_{ij})$ for benefit criteria and $\max(v_{ij})$ for cost criteria.

4. Separation Measures:

$S_i^+ = \sqrt{\sum (v_{ij} - v_j^+)^2}$ for PIS.

$S_i^- = \sqrt{\sum (v_{ij} - v_j^-)^2}$ for NIS.

5. Relative Closeness to the Ideal Solution:

$C_i^* = S_i^- / (S_i^+ + S_i^-)$, where C_i^* is the closeness coefficient of alternative i .

6. Ranking:

The alternatives are ranked in descending order of C_i^* .

Algorithm

1. Construct the decision matrix based on the criteria and alternatives.
2. Normalize the decision matrix.
3. Multiply the normalized decision matrix by the weight of each criterion to obtain the weighted normalized decision matrix.
4. Identify the positive ideal solution (PIS) and negative ideal solution (NIS).
5. Calculate the separation measures from PIS and NIS for each alternative.
6. Compute the relative closeness to the ideal solution for each alternative.
7. Rank the alternatives based on their closeness coefficients.

Linguistic Values

Table 1:Qualitative Linguistic Value Matrix for MCDM Analysis Using TOPSIS and DEMATEL Methods Across Multiple Criteria[14]

Unna med: 0	Crite ria 1	Crite ria 2	Crite ria 3	Crite ria 4	Crite ria 5	Crite ria 6	Crite ria 7	Crite ria 8	Crite ria 9	Crite ria 10	Crite ria 11	Crite ria 12	Crite ria 13
Alt 1	High	Very High	Medium	Very High	Very High	Low	Medium	Medium	Medium	Very High	High	Medium	Very High
Alt 2	Low	High	Low	High	Very High	Very Low	High	Low	Very High	High	Very Low	Very Low	Medium
Alt 3	Medium	Low	High	High	Medium	High	High	Very Low	Medium	Very High	Medium	Very High	Very Low
Alt 4	Low	High	Very Low	High	Low	Low	Very Low	Low	Very High	Low	High	High	High
Alt 5	High	Very High	Medium	Very Low	High	Low	High	Low	Low	High	Very High	Low	Low
Alt 6	High	Low	Low	High	High	Very Low	Very High	Very High	Low	Very High	Low	Very Low	High
Alt 7	High	High	Very High	Very Low	Very High	Very High	Very Low	Very Low	Very Low	Very Low	High	Medium	Medium
Alt 8	Very Low	Medium	Medium	Very Low	Medium	Very High	Low	Low	Very Low	High	Very Low	High	Low
Alt 9	Very Low	Very High	Medium	High	Medium	Medium	Very Low	Medium	Very High	Medium	Very Low	Very High	Low
Alt 10	Medium	Very Low	Low	Low	High	Very High	Medium	Very Low	High	Very High	High	Very High	Very High
Alt 11	Medium	Very High	High	Very High	Medium	Medium	High	Low	Low	Very High	Very Low	Very High	High
Alt 12	High	High	High	High	Medium	Low	High	Very Low	Very Low	Very Low	Very Low	Medium	Very Low
Alt 13	High	Very High	Very Low	Medium	Medium	Very Low	Very High	Very Low	Medium	Low	High	Medium	Very Low

Alt 14	High	Very Low	Very Low	Low	High	High	Low	Medium	Very Low	Very High	Very Low	Very Low	Medium
Alt 15	Very Low	Low	Low	High	Very High	Very Low	Very Low	Medium	Low	Very High	High	Low	High

The table 1 represents a linguistic value matrix implemented for multi-criteria decision-making (MCDM) methodologies, specifically the TOPSIS (Technique for Order Preference by Similarity to Ideal Solution) and DEMATEL (Decision-Making Trial and Evaluation Laboratory) methods. Each alternative (Alt 1 through Alt 15) is evaluated across various criteria (Criteria 1 to Criteria 13) using linguistic descriptors, such as "Very High," "High," "Medium," "Low," and "Very Low." These linguistic terms capture subjective assessments in a structured format, which is essential for MCDM approaches like TOPSIS and DEMATEL that require qualitative values to be converted into quantitative weights or influence levels. TOPSIS utilizes these linguistic values to identify the alternative closest to the ideal solution, considering both the best and worst cases, while DEMATEL uses them to assess the causal relationships between criteria, identifying which factors are most influential in the decision-making process[10]. This table, therefore, serves as a foundational input for converting qualitative judgments into actionable data, aiding in the systematic selection and prioritization of alternatives by combining the strengths of both MCDM methods[15].

Plithogenic Values

Table 2 :Plithogenic Value Matrix for MCDM using TOPSIS and DEMATEL

Unnamed: 0	Criteria 1	Criteria 2	Criteria 3	Criteria 4	Criteria 5	Criteria 6	Criteria 7	Criteria 8	Criteria 9	Criteria 10	Criteria 11	Criteria 12	Criteria 13
Alt 1	4	5	3	5	5	2	3	3	3	5	4	3	5
Alt 2	2	4	2	4	5	1	4	2	5	4	1	1	3
Alt 3	3	2	4	4	3	4	4	1	3	5	3	5	1
Alt 4	2	4	1	4	2	2	1	2	5	2	4	4	4
Alt 5	4	5	3	1	4	2	4	2	2	4	5	2	2
Alt 6	4	2	2	4	4	1	5	5	2	5	2	1	4
Alt 7	4	4	5	1	5	5	1	1	1	1	4	3	3
Alt 8	1	3	3	1	3	5	2	2	1	4	1	4	2
Alt 9	1	5	3	4	3	3	1	3	5	3	1	5	2
Alt 10	3	1	2	2	4	5	3	1	4	5	4	5	5
Alt 11	3	5	4	5	3	3	4	2	2	5	1	5	4
Alt 12	4	4	4	4	3	2	4	1	1	1	1	3	1
Alt 13	4	5	1	3	3	1	5	1	3	2	4	3	1
Alt 14	4	1	1	2	4	4	2	3	1	5	1	1	3
Alt 15	1	2	2	4	5	1	1	3	2	5	4	2	4

This table 2 displays a quantitative plithogenic value matrix applied in a multi-criteria decision-making (MCDM) context, specifically utilizing the TOPSIS (Technique for Order Preference by Similarity to Ideal Solution) and

DEMATEL (Decision-Making Trial and Evaluation Laboratory) methodologies. Each alternative (Alt 1 through Alt 15) is assessed across various criteria (Criteria 1 to Criteria 13) using plitogenic values, which provide a structured numerical rating for each criterion. These ratings range from 1 to 5, capturing various performance levels from low to high. Plitogenic values offer a robust way to incorporate uncertainty and complexity into the decision-making process, enhancing the assessment precision needed for MCDM techniques[16].

In the TOPSIS method, these numerical values serve as inputs to determine each alternative's proximity to an ideal solution by calculating both positive and negative ideal distances. DEMATEL uses these values to identify the causal relationships between criteria, allowing decision-makers to determine which criteria are most influential or dependent in the decision process. This quantitative matrix thus provides a clear, structured foundation for combining the strengths of both TOPSIS and DEMATEL methods, enabling systematic prioritization and selection among alternatives.

Defuzzified Values

Table 3 :Defuzzified Value Matrix for Lithogenic Neutrosophic MCDM using TOPSIS and DEMATEL

Unnam ed: 0	Crite ria 1	Crite ria 2	Crite ria 3	Crite ria 4	Crite ria 5	Crite ria 6	Crite ria 7	Crite ria 8	Crite ria 9	Crite ria 10	Crite ria 11	Crite ria 12	Crite ria 13
Alt 1	4	5	3	5	5	2	3	3	3	5	4	3	5
Alt 2	2	4	2	4	5	1	4	2	5	4	1	1	3
Alt 3	3	2	4	4	3	4	4	1	3	5	3	5	1
Alt 4	2	4	1	4	2	2	1	2	5	2	4	4	4
Alt 5	4	5	3	1	4	2	4	2	2	4	5	2	2
Alt 6	4	2	2	4	4	1	5	5	2	5	2	1	4
Alt 7	4	4	5	1	5	5	1	1	1	1	4	3	3
Alt 8	1	3	3	1	3	5	2	2	1	4	1	4	2
Alt 9	1	5	3	4	3	3	1	3	5	3	1	5	2
Alt 10	3	1	2	2	4	5	3	1	4	5	4	5	5
Alt 11	3	5	4	5	3	3	4	2	2	5	1	5	4
Alt 12	4	4	4	4	3	2	4	1	1	1	1	3	1
Alt 13	4	5	1	3	3	1	5	1	3	2	4	3	1
Alt 14	4	1	1	2	4	4	2	3	1	5	1	1	3
Alt 15	1	2	2	4	5	1	1	3	2	5	4	2	4

The table 3 presents a defuzzified value matrix tailored for a plithogenic neutrosophic multi-criteria decision-making (MCDM) analysis, employing the TOPSIS (Technique for Order Preference by Similarity to Ideal Solution) and DEMATEL (Decision-Making Trial and Evaluation Laboratory) methods. Each alternative (Alt 1 through Alt 15) is evaluated across various criteria (Criteria 1 to Criteria 13) using defuzzified numerical scores ranging from 1 to 5, which represent consolidated evaluations derived from initial linguistic or fuzzy values. This transformation into defuzzified values is essential for processing uncertain or imprecise data inherent in MCDM.

In this context, the defuzzified values provide crisp input data that allow TOPSIS to determine each alternative's proximity to an ideal solution, capturing both optimal and least-preferred positions. DEMATEL, meanwhile,

leverages these values to establish causal relationships among criteria, revealing influential and dependent factors in the decision framework. Together, the table's defuzzified values offer a clear foundation for systematic decision analysis, combining the strengths of both MCDM methods to prioritize and select the most suitable alternatives[17].

Decision Matrix

Table 4: Defuzzified Decision Matrix for Lithogenic Neutrosophic MCDM using TOPSIS and DEMATEL

U nn a m e d : o	Criter ia 1	Criter ia 2	Criter ia 3	Criter ia 4	Criter ia 5	Criter ia 6	Criter ia 7	Criter ia 8	Criter ia 9	Criter ia 10	Criter ia 11	Criter ia 12	Crite ria 13
Al t 1	0.080 8533 2633 27152 5	0.369 65445 60614 045	0.242 15993 8277 4259	0.80 31397 5637 9895 9	0.470 3006 3444 6038 4	0.983 4231 4089 4843	0.398 8244 4244 45531	0.816 4318 7321 9383 9	0.798 34512 4984 5511	0.150 71754 3965 4295	0.508 19877 6740 7187	0.695 8128 0679 0881 9	0.85 8358 8048 13719 8
Al t 2	0.325 9589 0520 1884 8	0.220 24104 75655 483	0.711 14953 2438 0178	0.80 9501 0461 39715 4	0.348 6659 87291 7294	0.09 61765 51091 4207 6	0.940 5232 6448 9604	0.397 5720 2108 7522 3	0.517 75135 0527 4801	0.837 71010 5907 328	0.675 69011 7039 2807	0.735 21611 9240 7721	0.20 9071 6207 37713 7
Al t 3	0.541 44797 3827 5658	0.695 78439 9345 0822	0.228 5500 21797 2997	0.174 9549 2709 5936 2	0.982 1683 4332 9435 6	0.516 6358 91271 0143	0.260 82917 4830 409	0.996 2536 9975 7924 3	0.965 41935 1288 7936	0.558 2934 5360 7097 6	0.882 6363 4318 9339 7	0.188 7071 0834 1379 4	0.278 8713 5259 2181 9
Al t 4	0.700 3578 2997 27713	0.846 66114 2238 3059	0.856 3242 9187 8092 4	0.40 4508 12712 21901	0.887 7700 9876 0959 8	0.85 0928 4487 67512 7	0.935 6349 9422 0947 5	0.785 3406 51113 9436	0.668 9882 54714 2286	0.580 6866 21436 4547	0.372 2827 66561 7431	0.94 0133 4424 5777 84	0.973 6638 3675 53173
Al t 5	0.283 9209 74737 4657	0.305 3638 6034 43934	0.485 61375 3586 2266	0.44 8424 1429 8624 73	0.994 4574 6261 0820 7	0.175 9252 5267 7345 4	0.018 0753 63615 5208 7	0.493 8937 15183 4346	0.178 8227 0922 1328 8	0.366 4687 8458 2859 9	0.744 17052 3056 5623	0.720 9399 2425 2129 3	0.30 8060 7918 5238 92
Al t 6	0.542 5402 3055 4899 3	0.508 81407 68387 6	0.636 33261 8185 8954	0.250 46181 8605 5841	0.589 8708 4756 0543 9	0.978 8928 5827 5009	0.486 74215 2959 4551	0.90 6098 78771 8554	0.434 3943 6551 0428 6	0.350 0784 0769 46757	0.645 1033 6203 0564 8	0.66 8924 0596 6309 96	0.86 4167 5650 7190 31
Al t 7	0.230 18526 82415 553	0.499 19337 9884 7523	0.572 0041 9920 91831	0.768 5540 1430 6309	0.043 6037 71754 43375	0.994 5505 1079 7341	0.469 94451 3990 9429	0.279 5603 4179 6758 6	0.883 4940 2226 6259	0.747 71877 3897 4139	0.953 0718 4702 3953 2	0.330 7503 0467 0513 7	0.552 7649 6683 5489 9
Al t 8	0.572 2924	0.980 33158	0.075 3462 5600	0.305 6970	0.190 91103	0.268 4748 5689	0.485 2798	0.372 6868 6709	0.394 6914 6680	0.844 21314	0.930 0168 3481	0.07 04161 3084	0.20 8918 71761

	69170 8383	37160 457	6128 21	1928 71818	11503 46	0156 8	74276 3157	4049 3	9472 2	0726 3114	0831 9	9543 9	5360 2
Alt 9	0.671 14351 6824 0506	0.358 64678 12961 639	0.254 1636 4906 9738 8	0.295 2905 8841 8938 7	0.322 5507 6423 8600 5	0.84 8669 7949 2467 44	0.136 62133 1442 0288	0.70 8910 9969 10118 6	0.552 8199 7690 7907 7	0.296 51014 36477 985	0.419 7808 5644 6276 5	0.256 2069 4359 4458 1	0.611 51371 0865 6805
Alt 10	0.081 59418 0400 2403 6	0.005 18486 27739 86776	0.627 8944 1494 8636 1	0.194 2739 53512 0422	0.070 9409 16999 9276 6	0.396 7838 27213 8884	0.050 7685 3103 9396 94	0.88 66171 4895 0659 9	0.027 61677 18737 047	0.578 8648 9550 75587	0.438 47412 3018 087	0.672 0261 3529 5199 4	0.32 8152 6674 74731 9
Alt 11	0.155 04161 67277 442	0.981 8408 88310 5311	0.838 9335 0206 9363 3	0.86 0404 61831 16753	0.250 25136 05158 641	0.03 8834 7344 2942 32	0.303 26551 4673 2228	0.537 0824 2719 6655 4	0.326 65124 1796 0409	0.827 8690 0378 7588 7	0.271 54291 58197 419	0.965 2518 3039 0769 8	0.457 2651 61613 7285
Alt 12	0.842 0230 75011 9814	0.194 3800 33994 873	0.411 3539 0505 6678 6	0.699 51221 0767 1938	0.138 3530 92417 8014	0.132 7454 2224 2969 8	0.969 5368 67114 159	0.714 5951 0417 9952 1	0.041 06751 6767 8757 9	0.398 8209 0144 4794 5	0.433 5207 3758 07421	0.744 0426 4299 91154	0.25 0860 5273 4666 12
Alt 13	0.184 33367 43313 7	0.080 87296 66171 9767	0.428 31447 4940 1078	0.68 8499 9007 6536 64	0.058 19359 5508 44361	0.915 21372 7626 4805	0.442 3522 29731 1044	0.239 7873 59157 4032	0.093 8732 9008 12917 5	0.182 8659 97107 3073	0.934 61399 73397 097	0.638 2705 9384 3350 4	0.516 6962 5742 6566 7
Alt 14	0.657 11132 8500 1668	0.435 67289 86778 911	0.730 0393 16561 8185	0.047 71612 7691 6487 9	0.566 03721 0494 0763	0.158 6464 4764 2491	0.120 16464 7805 6422	0.341 8796 6671 6401 6	0.091 7990 6581 3441 88	0.094 15698 8268 5601 2	0.311 4133 0939 12942	0.979 5105 2862 1508 6	0.175 3302 6988 9338 5
Alt 15	0.017 16110 18317 5024	0.763 36442 3003 9109	0.806 91297 7050 7795	0.346 3043 2108 9400 8	0.464 67381 2939 6114	0.649 7736 8264 2763 4	0.048 0589 24197 0337 3	0.949 14573 15913 859	0.886 6803 8729 8047 5	0.260 8936 23341 714	0.015 3045 4029 0384 75	0.933 4363 0807 9483	0.501 0398 8391 5259 2

This table 5 provides a defuzzified decision matrix specifically structured for plithogenic-based neutrosophic multi-criteria decision-making (MCDM) methods, employing the TOPSIS (Technique for Order Preference by Similarity to Ideal Solution) and DEMATEL (Decision-Making Trial and Evaluation Laboratory) methodologies. Each alternative (Alt 1 to Alt 15) is evaluated across multiple criteria (Criteria 1 through Criteria 13) using defuzzified numerical values derived from initial neutrosophic and lithogenic linguistic inputs. Neutrosophic sets, which capture degrees of truth, indeterminacy, and falsity, are converted to precise, crisp values that enable quantitative comparison[18].

In this matrix, the defuzzified values provide structured input data for MCDM processes. TOPSIS uses these values to calculate the relative proximity of each alternative to an ideal solution by considering both the positive and negative ideal distances, thus allowing for the identification of the best option. DEMATEL, on the other hand, leverages these values to analyze the causal relationships between criteria, identifying influential and dependent factors within the decision-making framework. This matrix format, by capturing the advantages of both TOPSIS and DEMATEL,

facilitates systematic prioritization of alternatives while accommodating the inherent uncertainties and complex interdependencies in real-world decision scenarios[19], [20].

TOPSIS Solution

Table 6 : Decision Matrix with Closeness Scores and Rankings for plithogenic Neutrosophic MCDM using TOPSIS

U n a m e: o	Crit eria 1	Crite ria 2	Crite ria 3	Crite ria 4	Crite ria 5	Crite ria 6	Crite ria 7	Crite ria 8	Crite ria 9	Crite ria 10	Crite ria 11	Crite ria 12	Crite ria 13	Clos enes s	R a n ki n g
Al t 1	1.41 4213 562	0.35 3553 3906	0.98 0331 5837	0.22 0241 047 6	0.47 030 0634 4460 384	0.98 3423 1408 948 4445 43	0.39 882 6431 8732 1249 5439 7767 806 880 4813 7198	0.81 6431 8732 1249 5439 7767 806 880 4813 7198	0.79 8345 1249 5439 7767 806 880 4813 7198	0.15 0717 8198 5812 835 9377 448 400 062 5	0.50 8198 5812 835 9377 448 400 062 5	0.69 5812 835 9377 448 400 062 5	0.85 835 9377 448 400 062 5	0.53 9377 448 400 062 5	1 1
Al t 2	0.5	0.22 0241 0475 6554 83	0.711 1495 3243 8017 8	0.80 9501 0461 3971 54	0.34 8665 6176 0523 7572 7751 7710 5690 5216 9071 396 3769 3981 411	0.09 6176 0523 7572 7751 7710 5690 5216 9071 396 3769 3981 411	0.94 0523 7572 7751 7710 5690 5216 9071 396 3769 3981 411	0.39 7572 7751 7710 5690 5216 9071 396 3769 3981 411	0.51 7751 7710 5690 5216 9071 396 3769 3981 411	0.83 7710 5690 5216 9071 396 3769 3981 411	0.67 5690 5216 9071 396 3769 3981 411	0.73 5216 9071 396 3769 3981 411	0.20 9071 396 3769 3981 411	0.68 396 3769 3981 411	1
Al t 3	0.5	0.69 5784 3993 4508 22	0.22 8550 0217 927 095 2943 7101 830 5792 8879 0709 8933 4137 9218 19	0.17 4954 2168 6635 082 6253 5419 8293 2636 8707 8871 5851 1643 8991 38	0.98 2168 6635 082 6253 5419 8293 2636 8707 8871 5851 1643 8991 38	0.51 6635 082 6253 5419 8293 2636 8707 8871 5851 1643 8991 38	0.26 082 6253 5419 8293 2636 8707 8871 5851 1643 8991 38	0.99 6253 5419 8293 2636 8707 8871 5851 1643 8991 38	0.96 5419 8293 2636 8707 8871 5851 1643 8991 38	0.55 8293 2636 8707 8871 5851 1643 8991 38	0.88 2636 8707 8871 5851 1643 8991 38	0.18 8707 8871 5851 1643 8991 38	0.27 8871 5851 1643 8991 38	0.61 5851 1643 8991 38	1 0
Al t 4	0.5	0.84 6661 1422 3830 59	0.85 6324 2918 7809 24	0.40 450 8127 1221 901	0.88 7770 092 5634 534 898 068 2282 0133 366 3891 604 5607 572	0.85 092 5634 534 898 068 2282 0133 366 3891 604 5607 572	0.93 5634 534 898 068 2282 0133 366 3891 604 5607 572	0.78 534 898 068 2282 0133 366 3891 604 5607 572	0.66 898 068 2282 0133 366 3891 604 5607 572	0.58 068 2282 0133 366 3891 604 5607 572	0.37 2282 0133 366 3891 604 5607 572	0.94 0133 366 3891 604 5607 572	0.97 366 3891 604 5607 572	0.94 3891 604 5607 572	3
Al t 5	0.5	0.30 5363 8603 4439 34	0.48 5613 7535 8622 66	0.44 842 4457 5925 8075 389 882 6468 4170 093 806 4251 5971 2516 74	0.99 4457 5925 8075 389 882 6468 4170 093 806 4251 5971 2516 74	0.17 5925 8075 389 882 6468 4170 093 806 4251 5971 2516 74	0.01 8075 389 882 6468 4170 093 806 4251 5971 2516 74	0.49 389 882 6468 4170 093 806 4251 5971 2516 74	0.17 882 6468 4170 093 806 4251 5971 2516 74	0.36 6468 4170 093 806 4251 5971 2516 74	0.74 4170 093 806 4251 5971 2516 74	0.72 093 806 4251 5971 2516 74	0.30 806 4251 5971 2516 74	0.94 4251 5971 2516 74	1 4
Al t 6	0.5	0.50 8814 0768 3876	0.63 6332 6181 8186 8475 285 1529 8787 3655 8407 6946 757	0.25 0461 8186 8475 285 1529 8787 3655 8407 6946 757	0.58 9870 889 6742 609 4394 007 5103 892 4167 7198 9335 550 038	0.97 889 6742 609 4394 007 5103 892 4167 7198 9335 550 038	0.48 6742 609 4394 007 5103 892 4167 7198 9335 550 038	0.90 609 4394 007 5103 892 4167 7198 9335 550 038	0.43 4394 007 5103 892 4167 7198 9335 550 038	0.35 007 5103 892 4167 7198 9335 550 038	0.64 5103 892 4167 7198 9335 550 038	0.66 892 4167 7198 9335 550 038	0.86 4167 7198 9335 550 038	0.86 7198 9335 550 038	7

Alt 7	0.5	0.49 9193 3798 8475 23	0.57 200 4199 2091 831	0.76 8554 0143 063 09	0.04 3603 7717 5443 375	0.99 4550 5107 9734 1	0.46 9944 5139 9094 29	0.27 956 0341 7967 586	0.88 3494 022 2662 59	0.74 7718 7738 9741 39	0.95 3071 8470 2395 32	0.33 075 030 467 0513 7	0.55 2764 966 835 489 9	0.63 640 3597 446 0113	9	
Alt 8	0.5	0.98 0331 5837 1604 57	0.07 5346 2560 0612 821	0.30 5697 0192 8718 18	0.19 0911 0311 5034 6	0.26 8474 856 8901 568	0.48 5279 8742 7631 57	0.37 268 686 709 404 93	0.39 4691 466 809 4722	0.84 4213 1407 2631 14	0.93 0016 8348 1083 19	0.07 0416 1308 4954 39	0.20 8918 7176 1536 02	0.80 094 929 468 239 97	2	
Alt 9	0.5	0.35 8646 7812 9616 39	0.25 4163 649 0697 388	0.29 529 058 8418 9387	0.32 2550 7642 386 005	0.84 866 9794 924 6744	0.13 6621 3314 4202 88	0.70 8910 996 9101 186	0.55 2819 9769 079 077	0.29 6510 1436 4779 85	0.41 9780 8564 4627 65	0.25 620 694 3594 4581	0.61 1513 7108 656 805	0.67 7168 3423 829 817	8	
Alt 10	0.5	0.00 5184 8627 7398 6776	0.62 7894 4149 4863 61	0.19 4273 9535 1204 22	0.07 094 0916 9999 2766	0.39 6783 8272 1388 84	0.05 0768 5310 3939 694	0.88 6617 1489 506 599	0.02 7616 7718 7370 47	0.57 886 4895 5075 587	0.43 8474 1230 1808 7	0.67 202 6135 2951 994	0.32 8152 6674 7473 19	0.57 3367 0416 7193 33	1 2	
Alt 11	0.5	0.98 1840 8883 1053 11	0.83 8933 502 069 3633	0.86 040 4618 3116 753	0.25 0251 3605 1586 41	0.03 883 4734 429 4232	0.30 3265 5146 7322 28	0.53 708 2427 1966 554	0.32 6651 2417 960 409	0.82 7869 1542 0037 87	0.27 1542 9158 1974 19	0.96 5251 830 3907 698	0.45 7265 1616 1372 85	0.12 850 035 3233 9102	1 5	
Alt 12	0.5	0.19 4380 0339 9487 3	0.41 1353 905 0566 786	0.69 9512 2107 6719 38	0.13 8353 0924 1780 14	0.13 2745 4222 429 698	0.96 9536 8671 1415 9	0.71 4595 1041 7995 21	0.04 1067 5167 6787 579	0.39 882 0901 4447 945	0.43 3520 7375 8074 21	0.74 404 264 299 9115 4	0.25 086 0527 346 6612	0.81 1204 1767 360 03	1 3	
Alt 13	0.5	0.08 0872 9666 1719 767	0.42 8314 4749 4010 78	0.68 849 990 0765 366 4	0.05 8193 5955 084 4361	0.91 5213 7276 264 805	0.44 2352 2297 3110 44	0.23 9787 3591 5740 32	0.09 3873 290 0812 9175	0.18 2865 9971 0730 73	0.93 4613 9973 3970 97	0.63 827 059 384 335 04	0.51 669 6257 426 5667	0.82 063 9475 7439 553	6	
Alt 14	0.65	7111 328 500 1668	0.43 5672 8986 7789 11	0.73 003 9316 5618 185	0.04 7716 1276 9164 879	0.56 6037 2104 9407 63	0.15 864 6447 642 491	0.12 0164 6478 0564 22	0.34 1879 6667 1640 16	0.09 1799 065 8134 4188	0.09 4156 988 2685 6012	0.311 4133 0939 1294 2	0.97 9510 528 6215 086	0.17 533 026 988 933 85	0.62 5939 6701 0157 28	4

Alt	0.01	0.76	0.80	0.34	0.46	0.64	0.04	0.94	0.88	0.26	0.01	0.93	0.50	0.82	5
1	7161	3364	6912	630	4673	9773	805	9145	668	089	5304	3436	1039	042	
2	1018	4230	9770	4321	8129	682	8924	7315	0387	3623	5402	308	883	684	
3	3175	0391	5077	089	3961	6427	1970	9138	298	3417	903	079	9152	3771	
4	024	09	95	400	14	634	3373	59	0475	14	8475	483	592	2681	
5				8											

This table 6 presents a decision matrix for multi-criteria decision-making (MCDM) using the TOPSIS (Technique for Order Preference by Similarity to Ideal Solution) method, where each alternative (Alt 1 through Alt 15) is evaluated across multiple criteria (Criteria 1 through Criteria 13) with normalized and defuzzified scores. In TOPSIS, the goal is to identify the best alternative by comparing each one's proximity to an ideal solution (the best possible values across all criteria) and an anti-ideal solution (the worst possible values). The values under each criterion are first normalized, making them dimensionless and comparable across different criteria. Using these normalized values, the distance of each alternative from the ideal and anti-ideal solutions is calculated, and a "closeness score" is then determined for each alternative. This score, which ranges from 0 to 1, reflects the relative proximity of each alternative to the ideal solution, with values closer to 1 indicating a stronger alignment with optimal performance. Based on these closeness scores, each alternative is ranked, with the highest-ranked option being the most favorable according to the criteria. This method provides a systematic, quantitative approach for decision-makers to rank and select the best alternative among multiple choices.

DEMATEL Analysis

Table 7: Criteria Prominence and Relation Matrix for DEMATEL Analysis in MCDM[21]

Criteria	Prominence	Relation
Criteria 1	0.2385968597903402	0.3549051904627206
Criteria 2	0.6798447799002458	0.9568008851264563
Criteria 3	0.7399087604473745	0.6767699044243033
Criteria 4	0.2382361524039794	0.4825209496426425
Criteria 5	0.3777288861762949	0.493025657771805
Criteria 6	0.5343274735305634	0.08328441119525964
Criteria 7	0.4965611906830777	0.09170414725848108
Criteria 8	0.3896180862192035	0.602440925901119
Criteria 9	0.2976351745093109	0.5537030523458008
Criteria 10	0.09998488716186338	0.212727895024229
Criteria 11	0.0534852967473689	0.9461945428816902
Criteria 12	0.9585414968831983	0.7812960504712025
Criteria 13	0.8471431440955898	0.113464602017448

This table 7 represents the criteria prominence and relation values calculated through the DEMATEL (Decision-Making Trial and Evaluation Laboratory) method, which is commonly applied in multi-criteria decision-making (MCDM) analyses to understand interdependencies among criteria. Each criterion (Criteria 1 to Criteria 13) is evaluated with two primary indicators: **Prominence** and **Relation**. The **Prominence** value measures the overall importance or influence of each criterion within the system, while the **Relation** value indicates whether the criterion tends to have more of a cause (positive influence) or effect (being influenced by other criteria) role within the decision-making framework[22].

Higher prominence values suggest that a criterion holds substantial weight in the decision process, either as an influencer or as one impacted by other criteria. The **Relation** values, meanwhile, distinguish the causality within the system: criteria with high relation scores typically act as influential factors, affecting other criteria, while those with lower relation values are primarily affected by other factors. Together, these values allow decision-makers to map out the network of causal relationships among criteria, identifying which criteria are critical drivers in the decision context and which are more dependent. By visualizing these relationships, DEMATEL aids in prioritizing the most influential criteria, enhancing the precision of decision-making in complex, interdependent scenarios[23], [24].

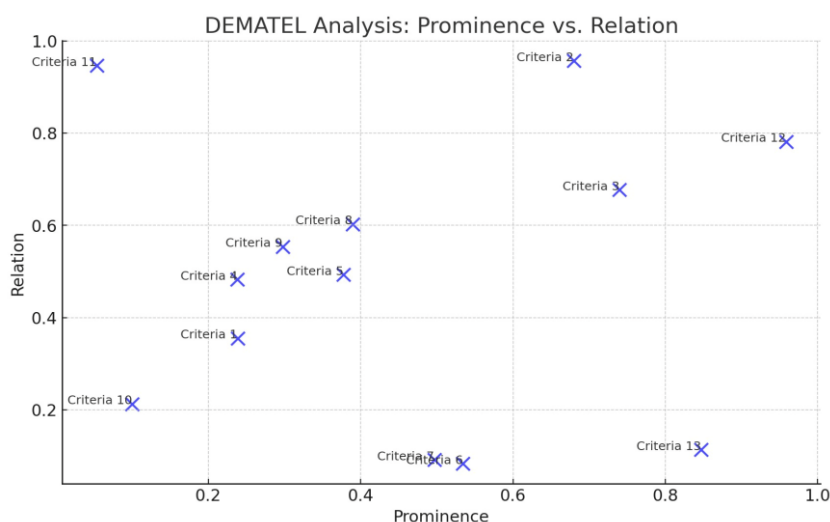


Figure 1 : prominence vs relations

Explanation of DEMATEL Analysis Graph

The graph above represents the results of a DEMATEL analysis, showing the 'Prominence' and 'Relation' values for various criteria[25]. In this context:

- **Prominence**: Indicates the overall importance or influence of a criterion. Higher prominence values suggest that the criterion plays a significant role in the overall evaluation.
- **Relation**: Reflects how strongly a criterion is interrelated with others. Higher relation values mean the criterion has more substantial connections or dependencies with other criteria.

Key Observations:

1. **Criteria with High Prominence and Relation**: Criteria such as 'Criteria 2' and 'Criteria 12' have high values for both prominence and relation, suggesting they are not only important but also have significant interdependencies with other criteria.
2. **Criteria with High Prominence but Low Relation**: Some criteria, like 'Criteria 13', have high prominence but lower relation values, indicating they are influential but less dependent on other criteria.
3. **Criteria with Low Prominence and Relation**: Criteria such as 'Criteria 11' and 'Criteria 10' have lower values for both metrics, suggesting they play a less critical role in the overall system.

This type of analysis helps decision-makers understand not just the importance of each criterion but also how they interact with each other. The graph allows for quick identification of key criteria that need to be managed carefully due to their high impact and strong interrelations.

CONCLUSION

In conclusion, this study demonstrates the effectiveness of integrating fuzzy MCDM methods, specifically TOPSIS and DEMATEL, within a neutrosophic framework to enhance decision-making in complex marketing strategy evaluations. By accommodating uncertainty, vagueness, and indeterminacy, these methods offer a more comprehensive approach to handling conflicting criteria and uncertain data. The comparative analysis highlights that

TOPSIS excels in efficiently ranking alternatives, making it suitable for straightforward decision-making scenarios, while DEMATEL provides deeper insights by revealing causal relationships among criteria, which is valuable for understanding complex interdependencies. The findings underscore the potential of neutrosophic MCDM approaches in improving decision-making processes across various domains. Future research can explore the integration of these methods with other advanced decision-making techniques to further refine their application and expand their usefulness in different contexts.

REFERENCE:

- [1] D. Pamučar, M. Mihajlović, R. Obradović, and P. Atanasković, "Novel approach to group multi-criteria decision making based on interval rough numbers: Hybrid DEMATEL-ANP-MAIRCA model," *Expert Syst Appl*, vol. 88, pp. 58–80, Dec. 2017, doi: 10.1016/J.ESWA.2017.06.037.
- [2] R. L. Eaton, "Hunting Behavior of the Cheetah," *J Wildl Manage*, vol. 34, no. 1, p. 56, Jan. 1970, doi: 10.2307/3799492.
- [3] D. Pamučar, G. Čirović, and D. Božanić, "Application of interval valued fuzzy-rough numbers in multi-criteria decision making: The IVFRN-MAIRCA model," *Yugoslav Journal of Operations Research*, vol. 29, no. 2, pp. 221–247, 2019, doi: 10.2298/YJOR180415011P.
- [4] H. M. I. Bloch, "Fuzzy mathematical morphology," *Ann Math Artif Intell*, vol. 10, pp. 55–84, 1994.
- [5] S. Amirghodsi, A. B. Naeini, and A. Makui, "An Integrated Delphi-DEMATEL-ELECTRE Method on Gray Numbers to Rank Technology Providers," *IEEE Trans Eng Manag*, vol. 69, no. 4, pp. 1348–1364, Aug. 2022, doi: 10.1109/TEM.2020.2980127.
- [6] M. Abdel-Basset and R. Mohamed, "A novel plithogenic TOPSIS- CRITIC model for sustainable supply chain risk management," *J Clean Prod*, vol. 247, Feb. 2020, doi: 10.1016/J.JCLEPRO.2019.119586.
- [7] B. D. Rouyendegh, A. Yildizbasi, and P. Üstünyer, "Intuitionistic Fuzzy TOPSIS method for green supplier selection problem," *Soft comput*, vol. 24, no. 3, pp. 2215–2228, Feb. 2020, doi: 10.1007/S00500-019-04054-8.
- [8] A. Shekhovtsov and W. Salabun, "A comparative case study of the VIKOR and TOPSIS rankings similarity," *Procedia Comput Sci*, vol. 176, pp. 3730–3740, Jan. 2020, doi: 10.1016/J.PROCS.2020.09.014.
- [9] A. K. Daiy, K. Y. Shen, J. Y. Huang, and T. M. Y. Lin, "A Hybrid MCDM Model for Evaluating Open Banking Business Partners," *Mathematics 2021, Vol. 9, Page 587*, vol. 9, no. 6, p. 587, Mar. 2021, doi: 10.3390/MATH9060587.
- [10] A. Özçil, A. Tuş, G. Z. Öztaş, E. A. Adalı, and T. Öztaş, "The Novel Integrated Model of Plithogenic Sets and MAIRCA Method for MCDM Problems," *Advances in Intelligent Systems and Computing*, vol. 1197 AISC, pp. 733–741, 2021, doi: 10.1007/978-3-030-51156-2_85.
- [11] F. Smarandache, "Plithogeny, Plithogenic Set, Logic, Probability and Statistics: A Short Review," *Journal of Computational and Cognitive Engineering*, no. July, 2022, doi: 10.47852/bonviewjccce2202191.
- [12] F. Smarandache, "Plithogeny, Plithogenic Set, Logic, Probability and Statistics: A Short Review," *Journal of Computational and Cognitive Engineering*, vol. 1, no. April, pp. 47–50, 2022, doi: 10.47852/bonviewjccce2202191.
- [13] F. Smarandache, "Plithogeny, Plithogenic Set, Logic, Probability and Statistics: A Short Review," *Journal of Computational and Cognitive Engineering*, vol. 1, no. April, pp. 47–50, 2022, doi: 10.47852/bonviewjccce2202191.
- [14] M. Abdel-Basset, R. Mohamed, A. E. N. H. Zaied, and F. Smarandache, "A hybrid plithogenic decision-making approach with quality function deployment for selecting supply chain sustainability metrics," *Symmetry (Basel)*, vol. 11, no. 7, Jul. 2019, doi: 10.3390/SYM11070903.
- [15] Y. Wu, L. Qin, C. Xu, and S. Ji, "Site selection of waste-to-energy (WtE) plant considering public satisfaction by an extended vikor method," *Math Probl Eng*, vol. 2018, 2018, doi: 10.1155/2018/5213504.
- [16] M. Keshavarz Ghorabae, "Developing an MCDM method for robot selection with interval type-2 fuzzy sets," *Robot Comput Integr Manuf*, vol. 37, pp. 221–232, Feb. 2016, doi: 10.1016/J.RCIM.2015.04.007.
- [17] D. D. J., "Fuzzy Sets and Systems," *Theory and applications.*, vol. 393, 1980, Accessed: Feb. 18, 2024. [Online]. Available: <https://cir.nii.ac.jp/crid/1573950399317120000.bib?lang=en>

- [18] H. S. Lee, G. H. Tzeng, W. Yeih, Y. J. Wang, and S. C. Yang, "Revised DEMATEL: Resolving the infeasibility of DEMATEL," *Appl Math Model*, vol. 37, no. 10–11, pp. 6746–6757, Jun. 2013, doi: 10.1016/J.APM.2013.01.016.
- [19] G. H. Tzeng, W. H. Chen, R. Yu, and M. L. Shih, "Fuzzy decision maps: A generalization of the DEMATEL methods," *Soft comput*, vol. 14, no. 11, pp. 1141–1150, Sep. 2010, doi: 10.1007/S00500-009-0507-0.
- [20] C. L. Lin and G. H. Tzeng, "A value-created system of science (technology) park by using DEMATEL," *Expert Syst Appl*, vol. 36, no. 6, pp. 9683–9697, Aug. 2009, doi: 10.1016/J.ESWA.2008.11.040.
- [21] P. T. W. Lee and C. W. Lin, "The cognition map of financial ratios of shipping companies using DEMATEL and MMDE," *Maritime Policy and Management*, vol. 40, no. 2, pp. 133–145, Mar. 2013, doi: 10.1080/03088839.2012.757374.
- [22] C. W. Li and G. H. Tzeng, "Identification of interrelationship of key customers' needs based on structural model for services/capabilities provided by a Semiconductor-Intellectual-Property Mall," *Appl Math Comput*, vol. 215, no. 6, pp. 2001–2010, Nov. 2009, doi: 10.1016/J.AMC.2009.07.059.
- [23] "Fuzzy Systems: Modeling and Control - Google Books." Accessed: Feb. 18, 2024. [Online]. Available: https://books.google.co.in/books?hl=en&lr=&id=1vrxBwAAQBAJ&oi=fnd&pg=PR15&dq=Sugeno+1970s+fuzzy&ots=z3zr7Q9DxR&sig=lxb3gVdblNIbgadpe2-_SQM_iuE&redir_esc=y#v=onepage&q=Sugeno%201970s%20fuzzy&f=false
- [24] M. Zare *et al.*, "Multi-criteria decision making approach in E-learning: A systematic review and classification," *Applied Soft Computing Journal*, vol. 45, pp. 108–128, Aug. 2016, doi: 10.1016/J.ASOC.2016.04.020.
- [25] C. Kahraman, S. Cevik Onar, B. Oztaysi, I. U. Sari, S. Cebi, and A. C. Tolga, Eds., "Intelligent and Fuzzy Techniques: Smart and Innovative Solutions," vol. 1197, 2021, doi: 10.1007/978-3-030-51156-2.