

# First-Principles Study of Half-Metallicity and Optical Properties in $\text{Co}_2\text{CrX}$ ( $X = \text{Al, Bi, Ge, Si}$ ) Heusler Compounds

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## ABSTRACT

In this work, we present a systematic first-principles investigation of the structural, electronic, magnetic, elastic, and optical properties of  $\text{Co}_2\text{CrX}$  ( $X = \text{Al, Bi, Ge, Si}$ ) full-Heusler compounds. The calculations are performed using the full-potential linearized augmented plane wave (FP-LAPW) method as implemented in the WIEN2k code within the framework of the generalized gradient approximation (GGA). Our results indicate that all studied compounds crystallize in the cubic  $L_{21}$  structure and exhibit half-metallic ferromagnetism with nearly 100% spin polarization, highlighting their strong potential for spintronic applications. Analysis of the electronic band structure and density of states reveals the presence of a band gap in the minority-spin channel, while the majority-spin states remain metallic at the Fermi level. The calculated total magnetic moments follow the Slater-Pauling rule and are predominantly contributed by Co and Cr atoms. Furthermore, optical properties including the dielectric function, reflectivity, absorption coefficient, optical conductivity, refractive index, and electron energy loss function are evaluated within the interband transition regime. The optical response demonstrates pronounced light-matter interaction and significant dispersion characteristics, suggesting suitability for optoelectronic applications.

**Keywords:** Heusler compounds, First-principles calculations, Half-metallicity, Spintronics, Optical properties.

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## 1. Introduction

Heusler compounds have attracted considerable scientific interest since their discovery in 1903, when German chemist Friedrich Heusler reported that the intermetallic compound  $\text{Cu}_2\text{MnAl}$  exhibits ferromagnetism despite being composed of non-magnetic elements [1]. This remarkable finding challenged existing theories of magnetism and laid the foundation for extensive research into this class of materials.

Subsequent studies in the early 20<sup>th</sup> century identified additional ferromagnetic Heusler alloys, including  $\text{Cu}_2\text{MnSn}$ ,  $\text{Cu}_2\text{MnSb}$ , and  $\text{Cu}_2\text{MnBi}$ , all of which crystallize in the cubic  $L_{21}$  structure. The ordered  $L_{21}$  phase, consisting of four interpenetrating face-centered cubic (fcc) sublattices, was systematically characterized by Bradley and Rogers in the 1930s, providing detailed insight into atomic site occupation [2].

A major breakthrough occurred in 1983 when Robert A. de Groot and co-workers predicted half-metallic ferromagnetism in the semi-Heusler compound NiMnSb [3]. In such materials, one spin channel exhibits metallic behavior while the other displays a band gap, resulting in 100% spin polarization at the Fermi level, an essential feature for spintronic applications.

At present, the Heusler family encompasses thousands of compounds, including full-, half-, inverse-, and quaternary Heuslers, which exhibit diverse magnetic and electronic properties. These materials are of significant interest due to their tunable band structures and potential applications in spintronics, thermoelectrics, and topological materials [4].

Among them, full-Heusler alloys with the general formula  $A_2BX$  (where A and B are transition metals and X is a main-group element) crystallize in the cubic  $L2_1$  structure with a 2:1:1 stoichiometry [5–7]. These compounds exhibit a wide range of physical properties, making them attractive candidates for multifunctional applications.

In the present work, we perform a detailed first-principles study of  $Co_2CrX$  (X = Al, Bi, Ge, Si) full-Heusler compounds. The calculations are conducted within the framework of density functional theory using the GGA approach as implemented in WIEN2k [8]. We systematically investigate their structural, electronic, magnetic, elastic, and optical properties to assess their suitability for advanced spintronic and optoelectronic applications.

## 2. Computational Methodology

The structural, electronic, optical, and magnetic properties of the  $Co_2CrX$  (X = Al, Bi, Ge, Si) full-Heusler compounds were investigated using the full-potential linearized augmented plane wave (FP-LAPW) method [9], as implemented in the WIEN2k package. The exchange-correlation effects were treated within the generalized gradient approximation (GGA) using the Perdew–Burke–Ernzerhof (PBE) functional [10]. Spin-orbit coupling (SOC) was included in all calculations to account for relativistic effects, which are particularly significant for heavier elements such as Bi.

Within the WIEN2k formalism, the core states were treated fully relativistically, while the valence states were described using a semi-relativistic approximation. The energy cutoff separating core and valence states was set to  $-6.0$  Ry. Brillouin zone integrations were performed using a Monkhorst–Pack k-point mesh comprising 1000 k-points for self-consistent field (SCF) calculations. For optical property calculations, a denser k-point grid of 10,000 points was employed to ensure improved numerical precision.

The basis set size was controlled by the parameter  $R_{MT} \times K_{max}$ , which was chosen to be 7.0, where  $R_{MT}$  represents the muffin-tin radius and  $K_{max}$  denotes the maximum magnitude of the reciprocal lattice vector. The self-consistency cycle was considered converged when the total energy difference between successive iterations was less than 0.0001 Ry. The wave functions inside the atomic spheres were expanded up to a maximum angular momentum quantum number of  $l_{max} = 10$ . In the interstitial region, the charge density and potential were expanded in a Fourier series with a cutoff parameter of  $G_{max} = 10$ .

The muffin-tin radii ( $R_{MT}$ ) for all atomic species were carefully selected to avoid sphere overlap while ensuring optimal representation of the basis functions. The corresponding values are listed in Table 1.

**Table 1: Muffin tin radius ( $R_{MT}$ ) for  $Co_2CrX$  (X = Al, Bi, Ge, Si)**

| Compound   | $R_{MT}$ (a.u) |      |      |
|------------|----------------|------|------|
|            | Co             | Cr   | X    |
| $Co_2CrAl$ | 2.37           | 2.27 | 2.16 |
| $Co_2CrBi$ | 2.14           | 2.13 | 2.26 |
| $Co_2CrGe$ | 2.22           | 2.11 | 2.12 |
| $Co_2CrSi$ | 2.26           | 2.16 | 1.90 |

To investigate the magnetic and spin-resolved electronic properties, both spin-up and spin-down channels were explicitly considered for all atomic species. A  $10 \times 10 \times 10$  Monkhorst–Pack  $k$ -point mesh was used for Brillouin zone sampling [11], ensuring a good compromise between computational efficiency and accuracy in total energy and magnetic moment calculations. During structural optimization, all atomic positions were relaxed without constraints in the  $x$ -,  $y$ -, and  $z$ -directions, allowing the system to reach its ground state geometry with minimal forces and stress.

### 3. Crystal Structure

The investigated  $\text{Co}_2\text{CrX}$  ( $X = \text{Al, Bi, Ge, Si}$ ) full-Heusler compounds crystallize in the cubic  $L2_1$  structure with space group  $Fm-3m$  (No. 225). The general formula of full-Heusler alloys is  $A_2BX$ , reflecting a 2:1:1 stoichiometry, where  $A$  and  $B$  are typically transition metals (d-block elements), and  $X$  is a main-group element (p-block metal or semimetal) [12,13].

The  $L2_1$  crystal structure consists of four interpenetrating face-centered cubic (fcc) sublattices. In the conventional unit cell, the atomic positions are given as:  $A_1$  at  $(\frac{1}{4}, \frac{1}{4}, \frac{1}{4})$ ,  $A_2$  at  $(\frac{3}{4}, \frac{3}{4}, \frac{3}{4})$ ,  $B$  at  $(0, 0, 0)$ , and  $X$  at  $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ . This highly symmetric atomic arrangement plays a crucial role in determining the electronic, magnetic, and mechanical properties of the compounds.

To determine the equilibrium structural parameters, volume optimization was performed by fitting the calculated total energy as a function of volume to the Murnaghan equation of state [14]. This equation establishes the relationship between total energy  $E$  and volume  $V$  as follows:

$$E(V) = E_0 + \frac{B_0 V}{B'_0 (B'_0 - 1)} \left[ \left( \frac{V_0}{V} \right)^{B'_0 - 1} + 1 \right] - \frac{B_0 V_0}{B'_0 - 1}$$

where  $E_0$  is the minimum energy at  $T = 0 \text{ K}$ ,  $V_0$  is the equilibrium volume,  $B_0$  is the bulk modulus,  $B'_0$  is the pressure derivative of the bulk modulus.

The results of the structural optimization are shown in Figure 1. The calculated values of the optimized lattice parameters, minimum energy, bulk modulus, and its pressure derivative are summarized in Table 2.

**Table 2: Lattice Parameter, Bulk modulus, Equilibrium energy and Pressure derivative for  $\text{Co}_2\text{CrX}$  ( $X = \text{Al, Bi, Ge, Si}$ )**

|                          | Lattice Constants $a_0$ (Å) |                       | Bulk modulus (GPa) |           | Equilibrium energy ( $E_0$ ) | Pressure derivative |
|--------------------------|-----------------------------|-----------------------|--------------------|-----------|------------------------------|---------------------|
|                          | Our Calc.                   | Others                | Our Calc.          | Others    |                              |                     |
| $\text{Co}_2\text{CrAl}$ | 5.710                       | 5.73[15]<br>5.727[16] | 196.671            | 195[23]   | -8142.954                    | 4.923               |
| $\text{Co}_2\text{CrBi}$ | 5.649                       | 5.65[17]<br>5.63[18]  | 396.351            | 406[24]   | -50824.088                   | -0.944              |
| $\text{Co}_2\text{CrGe}$ | 5.742                       | 5.77[19]<br>5.74[20]  | 217.234            | 250.4[25] | -11856.872                   | 4.132               |
| $\text{Co}_2\text{CrSi}$ | 5.731                       | 5.87[21]<br>5.87[22]  | 392.060            | 405.5[26] | -48241.791                   | 0.143               |

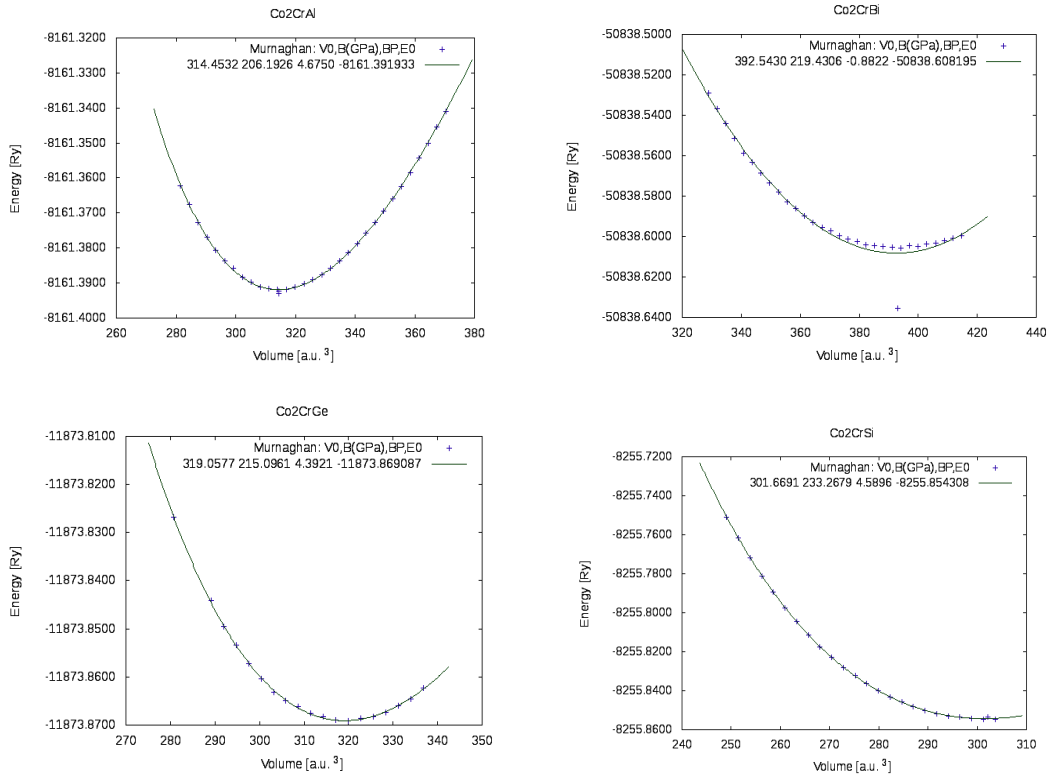


Fig. 1: Volume optimization curve for the lattice parameters

#### 4. Electronic properties

Spintronics has emerged as a transformative paradigm in modern electronics, enabling devices that exploit not only the charge of electrons but also their intrinsic spin. This dual functionality offers significant advantages, including enhanced data processing speeds, reduced energy consumption, and lower heat dissipation. A key class of materials in this field is half-metallic ferromagnets, which exhibit 100% spin polarization at the Fermi level.

Full-Heusler alloys, particularly Co<sub>2</sub>CrX (X = Al, Bi, Ge, Si), have attracted considerable attention due to their potential in spintronic applications. In the present study, spin-polarized calculations were performed within the generalized gradient approximation (GGA) at the optimized lattice parameters. The electronic structure analysis indicates that these compounds display metallic behavior in one spin channel, while the opposite spin channel exhibits a semiconducting gap, an essential characteristic of half-metallicity. The degree of spin polarization at the Fermi level is quantified using the following relation:

$$P_n = \frac{\rho \uparrow (E_F) - \rho \downarrow (E_F)}{\rho \uparrow (E_F) + \rho \downarrow (E_F)}$$

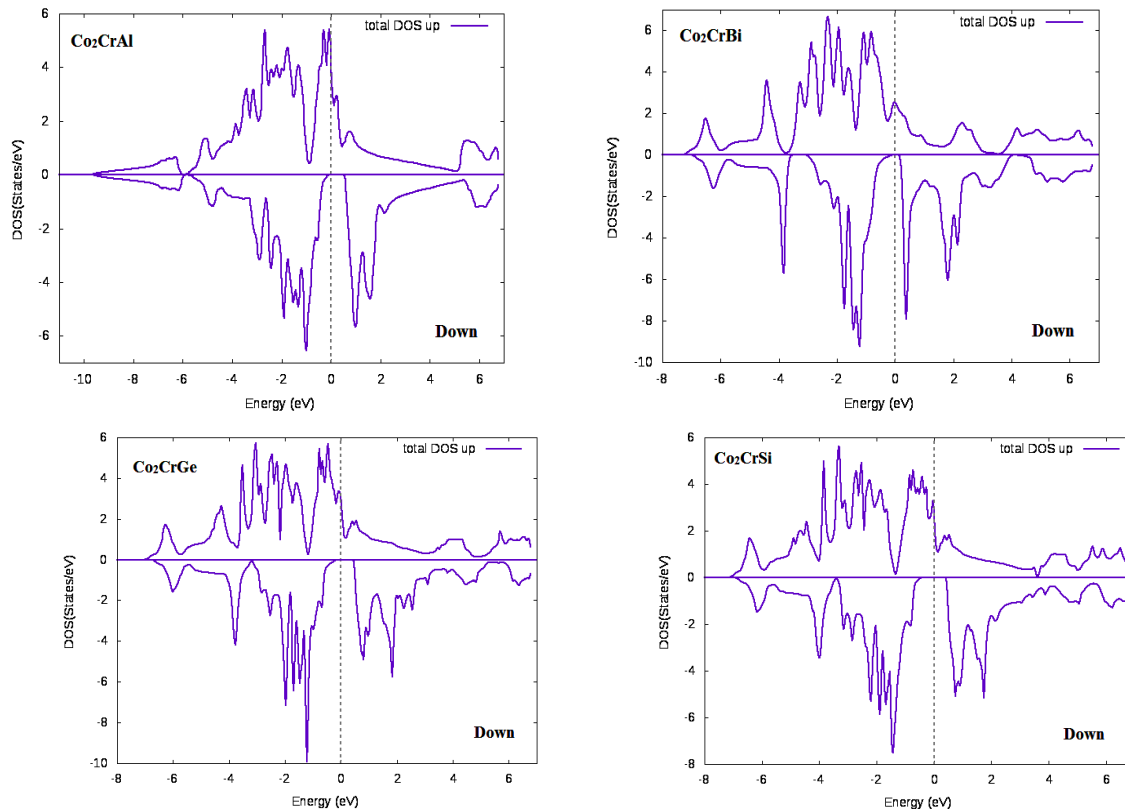
where  $\rho \uparrow (E_F)$  and  $\rho \downarrow (E_F)$  denote the densities of states at the Fermi level for spin-up and spin-down electrons, respectively. A value of  $P_n = \pm 1$  corresponds to complete spin polarization, indicating that only one spin channel contributes to electrical conduction. Such behavior is highly desirable for applications in magnetic sensors, spin transistors, and non-volatile memory devices. Conversely,  $P_n = 0$  signifies the absence of spin polarization, typical of paramagnetic or antiferromagnetic systems, even below the magnetic transition temperature [27].

To further elucidate the electronic characteristics of  $\text{Co}_2\text{CrX}$  compounds, the density of states (DOS) and band structures were analyzed using the WIEN2k code. The results reveal the presence of a band gap in the minority-spin channel, with calculated values of 0.696 eV (Al), 0.258 eV (Bi), 0.603 eV (Ge), and 0.849 eV (Si). These findings confirm the half-metallic nature of the studied compounds and their associated 100% spin polarization.

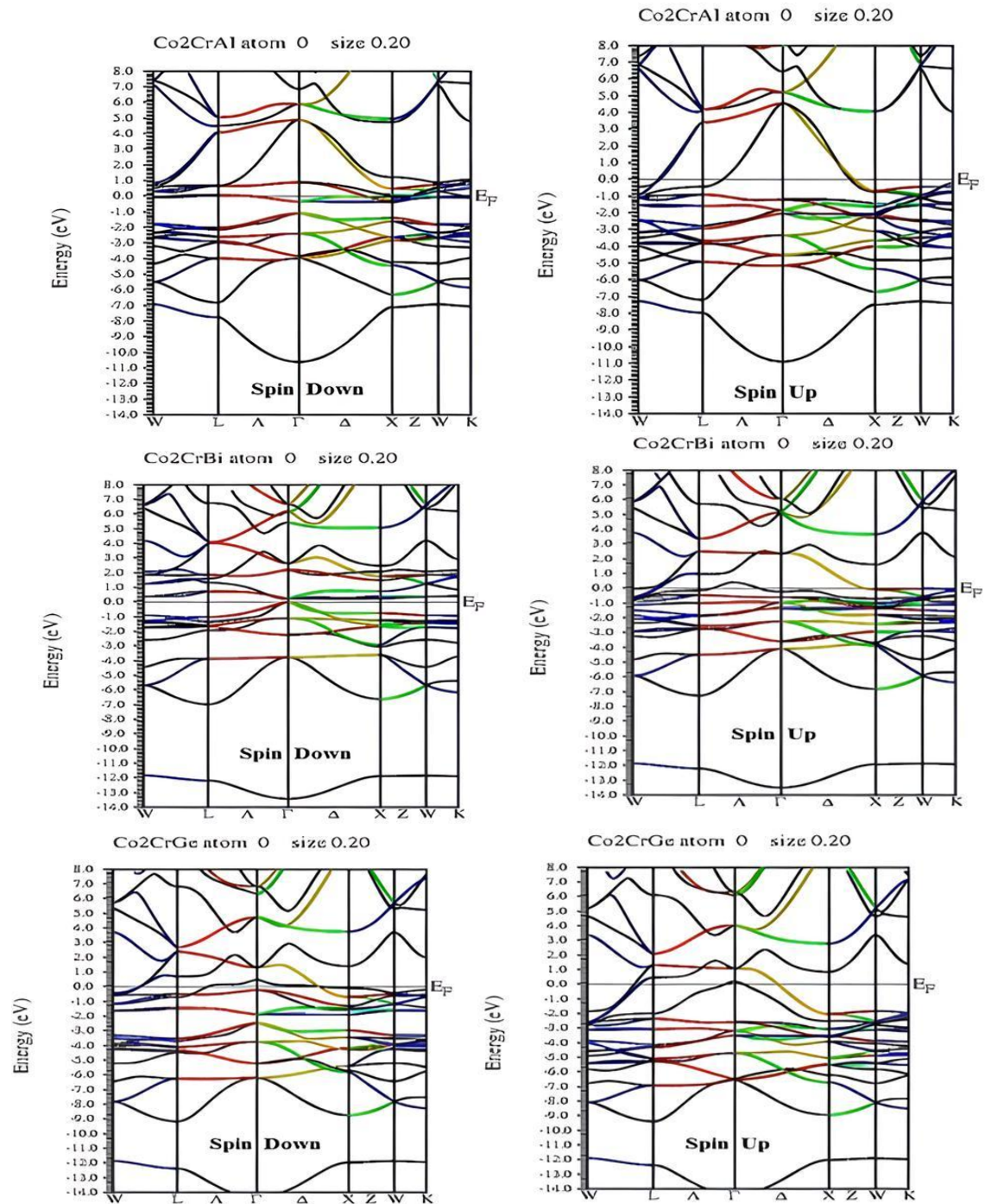
A summary of the calculated band gaps and corresponding spin polarization values is provided in Table 3, while Figures 2 and 3 illustrate the detailed band structures and density of states.

**Table 3: Energy gap and spin polarization of  $\text{Co}_2\text{CrX}$  (X= Al, Bi, Ge, Si) Compounds**

|                          | Energy gap $E_g$ (eV) |           | Spin polarization |
|--------------------------|-----------------------|-----------|-------------------|
|                          | Up spin               | Down spin |                   |
| $\text{Co}_2\text{CrAl}$ | 0.0                   | 0.696     | 100%              |
| $\text{Co}_2\text{CrBi}$ | 0.0                   | 0.258     | 100%              |
| $\text{Co}_2\text{CrGe}$ | 0.0                   | 0.603     | 100%              |
| $\text{Co}_2\text{CrSi}$ | 0.0                   | 0.849     | 100%              |



**Fig. 2: DOS of  $\text{Co}_2\text{CrX}$  (X= Al, Bi, Ge, Si) using WIEN2k code**



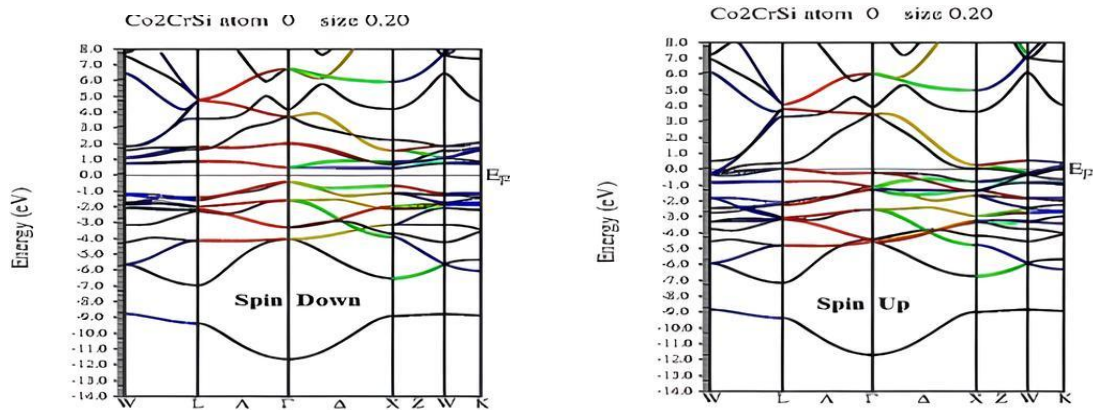


Fig. 3: Band Structure of Co<sub>2</sub>CrX (X = Al, Bi, Ge, Si) using WIEN2k code

### 5. Magnetic properties

The magnetic behavior of Heusler alloys is strongly governed by their valence electron concentration (VEC). A critical threshold occurs at 24 valence electrons per formula unit, where compounds typically exhibit non-magnetic semiconducting behavior. For instance, Fe<sub>2</sub>VAL, a well-known Heusler compound, possesses exactly 24 valence electrons and displays non-magnetic characteristics, with Fe atoms remaining in a non-magnetic state [27,28].

In contrast, Co<sub>2</sub>BX-type Heusler alloys generally contain more than 24 valence electrons and exhibit ferromagnetic behavior that follows the Slater-Pauling rule. This empirical relationship connects the total number of valence electrons ( $Z_t$ ) to the total magnetic moment ( $M$ ) per formula unit:

$$M = Z_t - 24$$

In half-metallic ferromagnetic Heusler compounds, the Curie temperature is often found to increase approximately linearly with the valence electron count, with an estimated increment of about 175 K per additional valence electron. For example, Co<sub>2</sub>CrAl, which has 27 valence electrons, exhibits a total magnetic moment of 3  $\mu_B$  per formula unit. This compound is ferromagnetic, with the magnetic moment primarily localized on the Co atoms, and shows a Curie temperature of approximately 525 K.

For the Co<sub>2</sub>CrX (X = Al, Bi, Ge, Si) compounds investigated in this work, the calculated valence electron counts are 27, 29, 28, and 28, respectively. According to the Slater-Pauling rule, these correspond to total magnetic moments of 3.0, 5.0, 4.0, and 4.0  $\mu_B$  per formula unit. The computed results, obtained using the FP-LAPW method within the WIEN2k framework and the GGA approximation, show excellent agreement with these predictions. A summary of the calculated magnetic moments is presented in Table 4.

Further analysis indicates that the dominant contribution to the total magnetic moment arises from the Co and Cr atomic sites, while the X-site atoms contribute only marginally. Additionally, an increase in the valence electron count at the X-site enhances the magnetic moments at the Co and Cr sites, thereby strengthening the overall ferromagnetic behavior of the compounds.

Table 4: Total magnetic moments of the compounds Co<sub>2</sub>CrX (X= Al, Bi, Ge, Si).

| Compound             | $Z_t$ | Magnetic moment ( $\mu_B$ ) |                |
|----------------------|-------|-----------------------------|----------------|
|                      |       | Calculated                  | Slater-Pauling |
| Co <sub>2</sub> CrAl | 27    | 3.01                        | 3.00           |
| Co <sub>2</sub> CrBi | 29    | 5.02                        | 5.00           |

|                      |    |      |      |
|----------------------|----|------|------|
| Co <sub>2</sub> CrGe | 28 | 4.01 | 4.00 |
| Co <sub>2</sub> CrSi | 28 | 4.01 | 4.00 |

### 6. Optical properties

Optical properties play a crucial role in determining the suitability of materials for optoelectronic applications. In this section, we analyze the optical response of Co<sub>2</sub>CrX (X = Al, Bi, Ge, Si) full-Heusler compounds through key parameters, including the dielectric function, optical conductivity, reflectivity, extinction coefficient, absorption coefficient, and electron energy loss function (EELF), all evaluated as functions of photon energy.

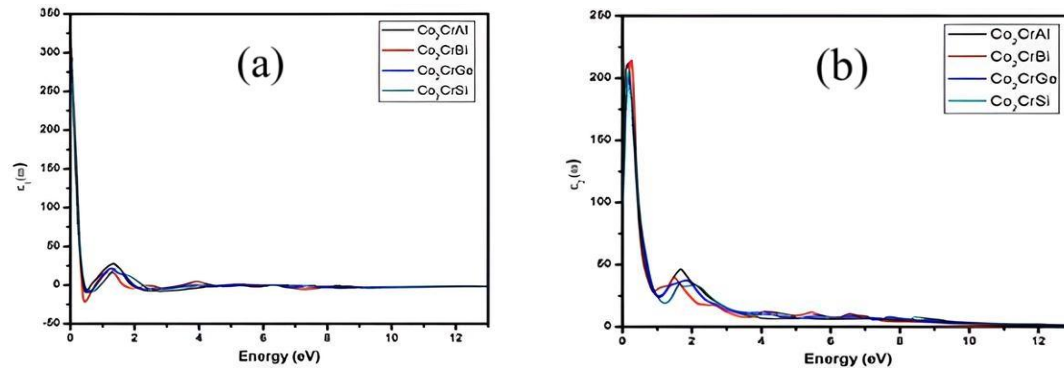
#### 6.1 Dielectric Function

The interaction of electromagnetic radiation with a material is described by the complex dielectric function, given by:

$$\varepsilon(\omega) = \varepsilon_1(\omega) + i\varepsilon_2(\omega)$$

where  $\varepsilon_1(\omega)$  represents the real part associated with polarization and dispersion, and denotes the imaginary part corresponding to optical absorption and energy dissipation [29]. The optical spectra are primarily governed by interband electronic transitions.

The calculated imaginary part of the dielectric function exhibits a dominant peak in the infrared region (0.08–0.31 eV), followed by smaller peaks in the visible range (1.13–1.86 eV). At zero photon energy, the static dielectric constants are obtained as follows: Co<sub>2</sub>CrAl:  $\varepsilon_1(0) = 311.85$ ,  $\varepsilon_2(0) = 140.75$ ; Co<sub>2</sub>CrBi:  $\varepsilon_1(0) = 300.15$ ,  $\varepsilon_2(0) = 112.10$ ; Co<sub>2</sub>CrGe:  $\varepsilon_1(0) = 287.60$ ,  $\varepsilon_2(0) = 105.90$  and Co<sub>2</sub>CrSi:  $\varepsilon_1(0) = 291.10$ ,  $\varepsilon_2(0) = 98.80$ .



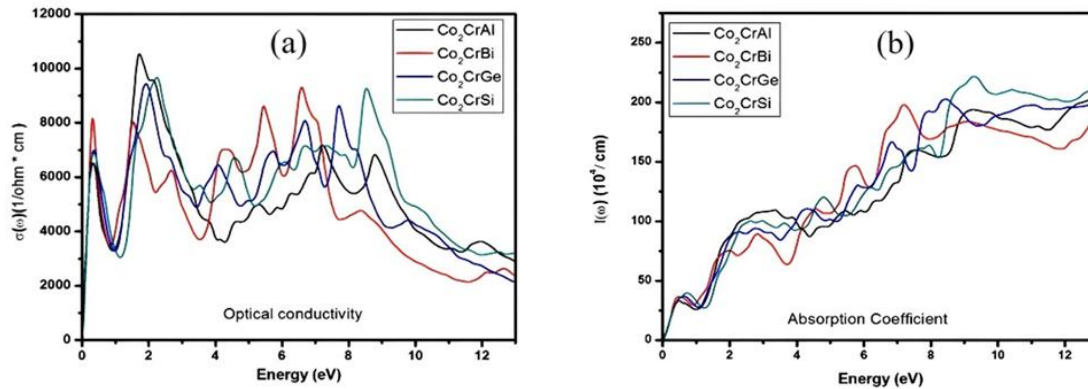
**Fig. 4: Calculated optical parameters (a) real part of dielectric function (b) imaginary part of dielectric function for Co<sub>2</sub>CrX (X = Al, Bi, Ge, Si).**

#### 6.2 Optical Conductivity

Optical conductivity provides insight into charge carrier dynamics under an applied electromagnetic field. The calculated spectra display prominent peaks in the energy range of 5.4–8.6 eV, with a notable feature between 1.6 and 2.3 eV. Additional peaks observed in the infrared region (0.18–0.50 eV and 1.38–1.88 eV) indicate strong interband electronic transitions.

#### 6.3 Absorption Coefficient

The absorption coefficient increases with photon energy, spanning the visible to ultraviolet regions. Maximum absorption peaks are observed between 7.50 and 8.75 eV for all compounds, indicating strong photon absorption in this energy range and suggesting their suitability for ultraviolet optoelectronic applications.



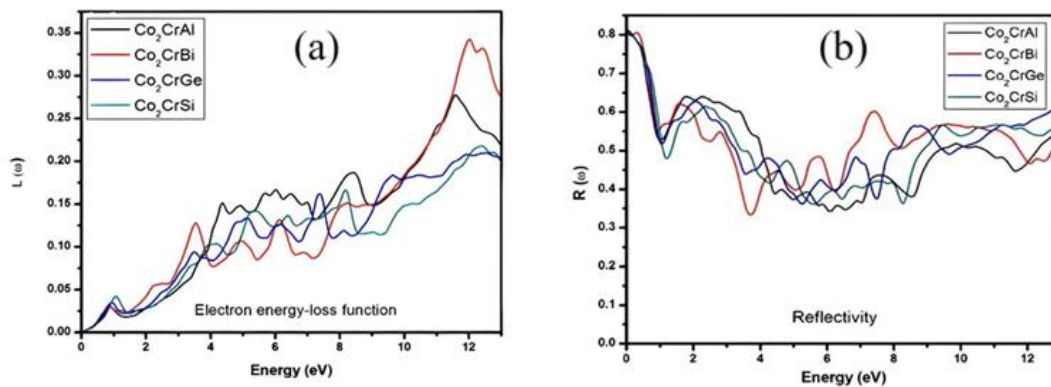
**Fig. 5: Calculated optical parameters (a) optical conductivity (b) absorption coefficient for  $\text{Co}_2\text{CrX}$  ( $X = \text{Al, Bi, Ge, Si}$ ).**

### 6.4 Electron Energy Loss Function

The electron energy loss function (EELF) characterizes the energy loss of fast electrons traversing the material. A pronounced peak corresponding to the plasma frequency marks the transition from metallic to dielectric behavior. Below this frequency, the material exhibits metallic characteristics, whereas dielectric behavior dominates above it. The EELF increases from the infrared to ultraviolet region, with maximum energy loss occurring between 12 and 13 eV.

### 6.5 Extinction Coefficient

The extinction coefficient spectrum shows a strong peak in the infrared region (0.12–0.54 eV), followed by a gradual decrease. A secondary peak appears in the visible region (1.16–2.59 eV), along with a weaker feature near 8 eV in the ultraviolet range.



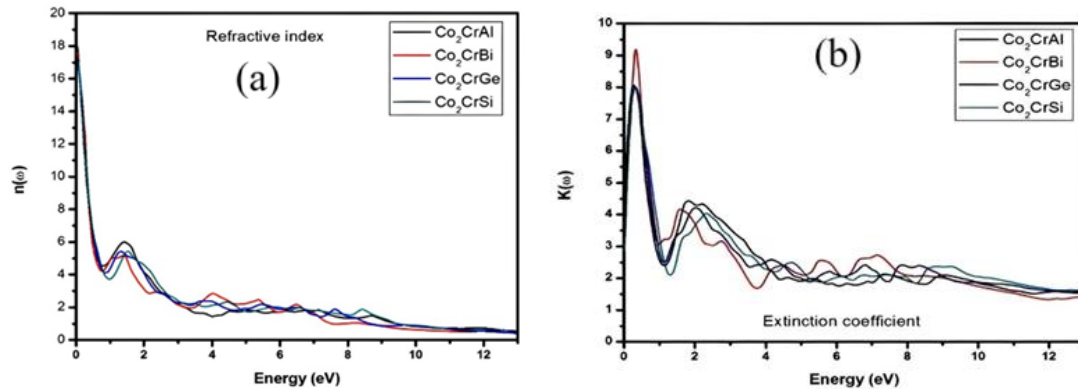
**Fig. 6: Calculated optical parameters (a) electron energy-loss function (b) reflectivity for  $\text{Co}_2\text{CrX}$  ( $X = \text{Al, Bi, Ge, Si}$ ).**

### 6.6 Reflectivity

Reflectivity determines the fraction of incident electromagnetic radiation reflected from the material surface. The static reflectivity values are calculated as:  $\text{Co}_2\text{CrAl}$  (0.808),  $\text{Co}_2\text{CrBi}$  (0.804),  $\text{Co}_2\text{CrGe}$  (0.800), and  $\text{Co}_2\text{CrSi}$  (0.796). Reflectivity initially decreases with increasing photon energy, reaching a minimum near 2 eV, and subsequently increases toward the ultraviolet region (~8.3 eV). This trend is inversely related to the absorption coefficient and is consistent with typical optical behavior.

### 6.7 Refractive Index

The refractive index is a key optical parameter governing light propagation, dispersion, and total internal reflection. At zero frequency, the calculated refractive indices are:  $\text{Co}_2\text{CrAl}$  (18.09),  $\text{Co}_2\text{CrBi}$  (17.63),  $\text{Co}_2\text{CrGe}$  (17.28), and  $\text{Co}_2\text{CrSi}$  (17.26). These high values indicate strong light–matter interaction and significant dispersion potential in these compounds.



**Fig. 7: Calculated optical parameters (a) refractive index and (b) extinction coefficient for  $\text{Co}_2\text{CrX}$  ( $X = \text{Al, Bi, Ge, Si}$ ).**

## 7. Conclusions

In this study, a comprehensive first-principles investigation of the structural, electronic, magnetic, elastic, and optical properties of  $\text{Co}_2\text{CrX}$  ( $X = \text{Al, Bi, Ge, Si}$ ) full-Heusler compounds has been carried out using the FP-LAPW method within the WIEN2k framework, employing the generalized gradient approximation (GGA) for exchange–correlation effects.

The electronic structure analysis, based on band structure and density of states calculations, confirms that all studied compounds exhibit half-metallic behavior with 100% spin polarization. The compounds crystallize in the cubic  $L2_1$  structure and are found to be energetically stable. The calculated magnetic moments follow the Slater–Pauling rule, demonstrating excellent agreement with theoretical predictions.

The optical properties, including dielectric function, optical conductivity, reflectivity, refractive index, absorption coefficient, extinction coefficient, and electron energy loss function, have been systematically analyzed over a wide photon energy range. The results indicate strong interband transitions, high optical absorption, and significant dispersion characteristics.

Overall, the  $\text{Co}_2\text{CrX}$  ( $X = \text{Al, Bi, Ge, Si}$ ) compounds exhibit a unique combination of half-metallicity, robust ferromagnetism, and favorable optical properties, making them promising candidates for future spintronic and optoelectronic applications.

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